

# **Nonlinear transport in GaAs heavily doped quantum wells at large filling factors**

*Institute of Semiconductor Physics, Novosibirsk, Russia*

**A. A. Bykov, A. I. Toropov**

*Physics Department, City College of the City University of New York, USA*

**S. A. Vitkalov**

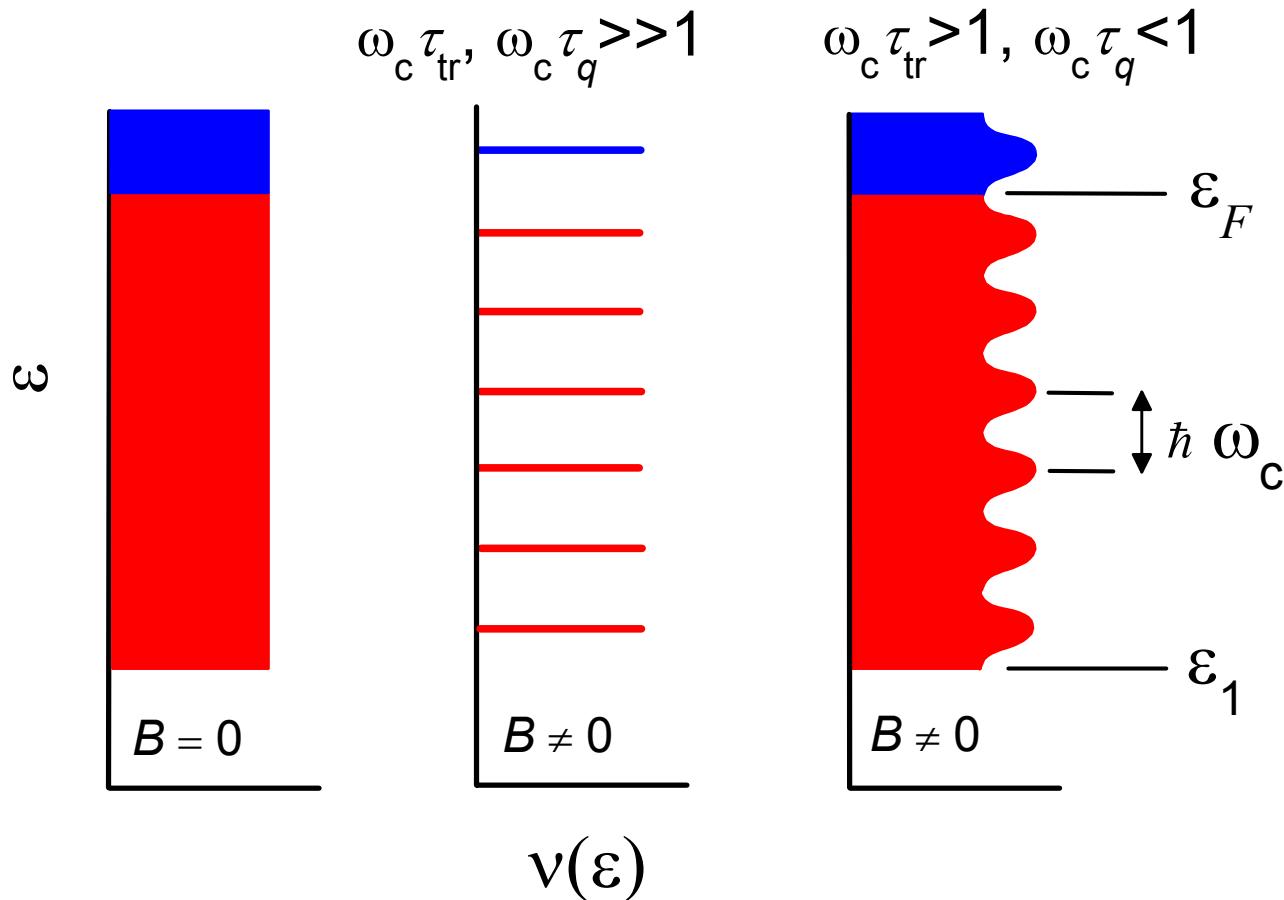
## Outline

1. Introduction
2. Experiment
3. Results
4. Conclusion

Работа  
проводилась  
при  
финансовой  
поддержке  
РФФИ

# 1. Introduction

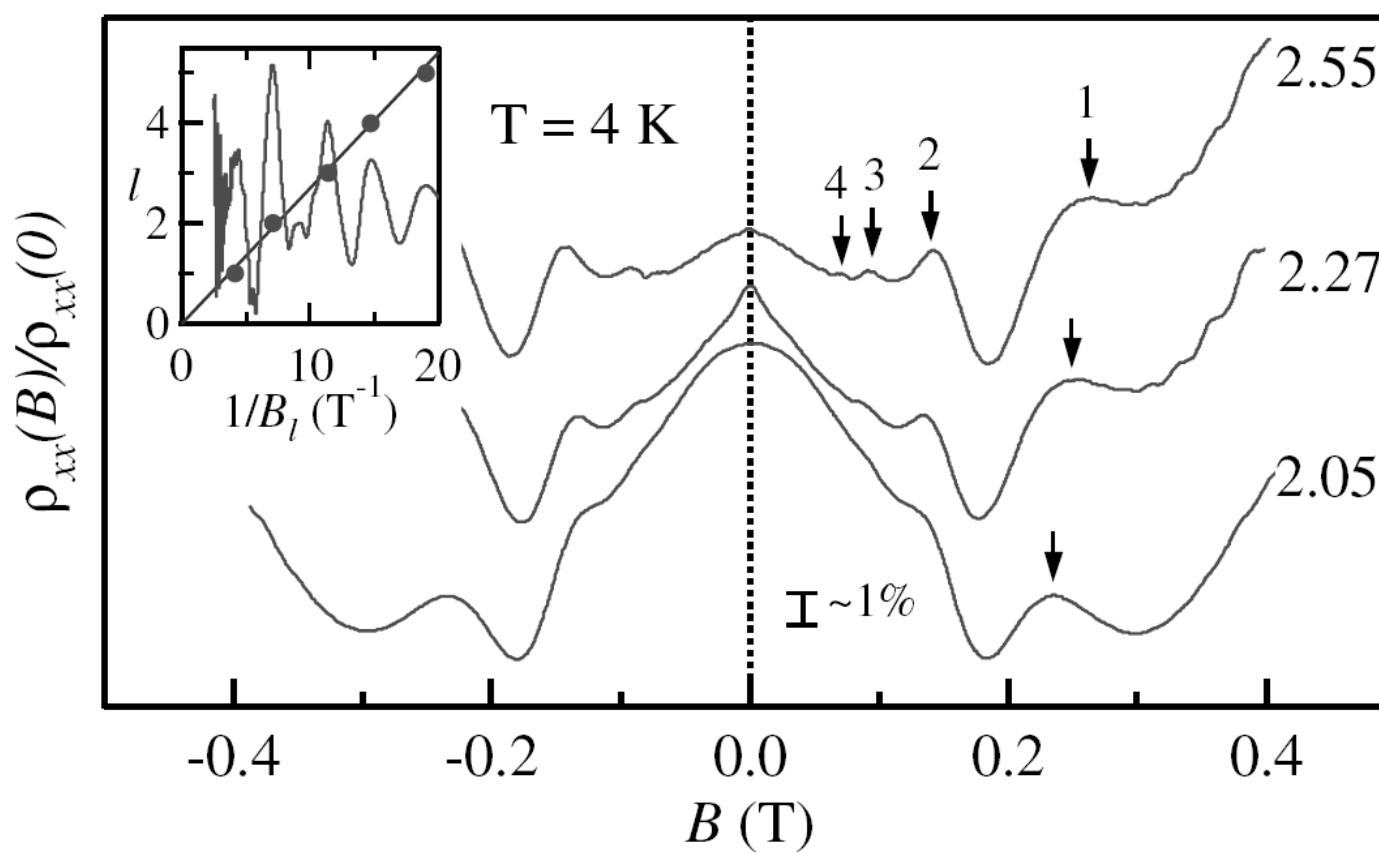
$$\varepsilon_F \gg \hbar \omega_c$$



$$\sigma_{xx} = \int \sigma_{\text{dc}}(\varepsilon) [-\partial_\varepsilon f_T(\varepsilon)] d\varepsilon$$

# Phonon-Induced Resistance Oscillations (PIRO, $\omega_S/\omega_c$ -oscillations)

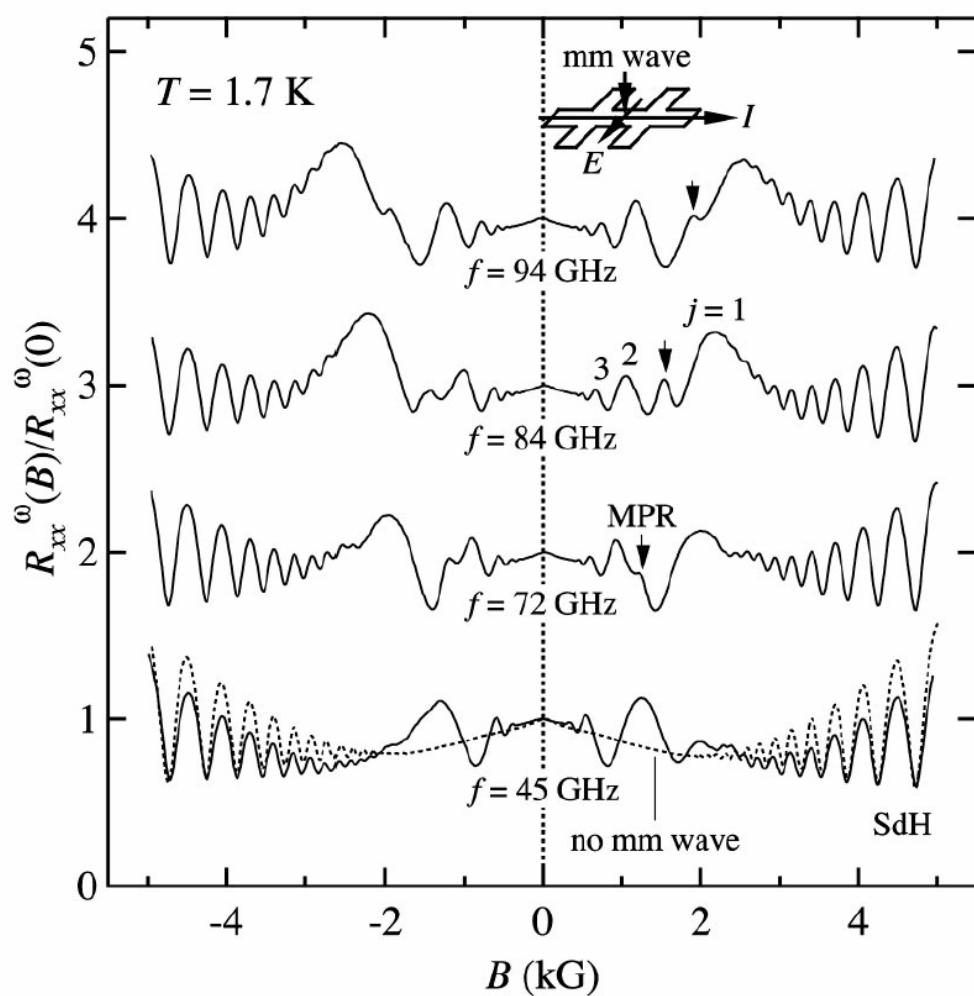
M. A. Zudov et al.  
PRL, 86, 3614 (2001)



$$2k_F u_S = l\omega_c$$

FIG. 1.  $\rho_{xx}(B)/\rho_{xx}(0)$  traces (shifted vertically for clarity) are shown for three densities  $n_e$  of 2.05, 2.27, and  $2.55 \times 10^{11} \text{ cm}^{-2}$ , respectively; arrows indicate the maxima for  $l = 1, 2, 3, 4$  and the shift of the primary ( $l = 1$ ) peak with increasing  $n_e$ . Inset shows that the oscillations are periodic in  $1/B$ .

# Microwave-Induced Resistance Oscillations (MIRO, $\omega/\omega_c$ -oscillations)



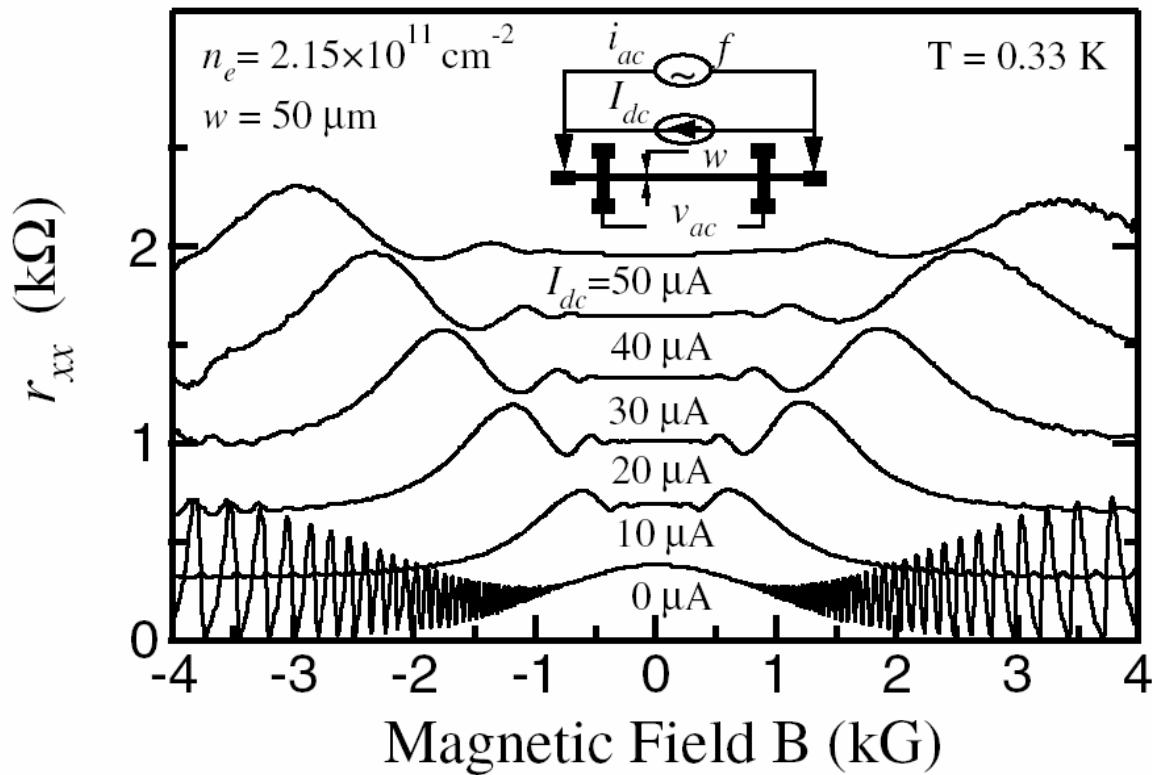
$$\omega = j\omega_c$$

FIG. 1. Normalized magnetoresistance from  $200 \mu\text{m}$  Hall bar with millimeterwave illumination on (solid lines) and off (dotted line) for selected frequencies. The traces are offset vertically for clarity. The arrows mark the magnetoplasmon resonance signal. The difference in SdH amplitudes between illumination on ( $T \approx 1.7$  K) and off ( $T \approx 1.5$  K) traces is due to a nonresonant heating of the 2DEG by the millimeterwave radiation.

**M. A. Zudov et al.**  
PRB, **64**, 201311(R) (2001)

# Hall Field-Induced Resistance Oscillations

## (HIRO, $\omega_H/\omega_c$ -oscillations)

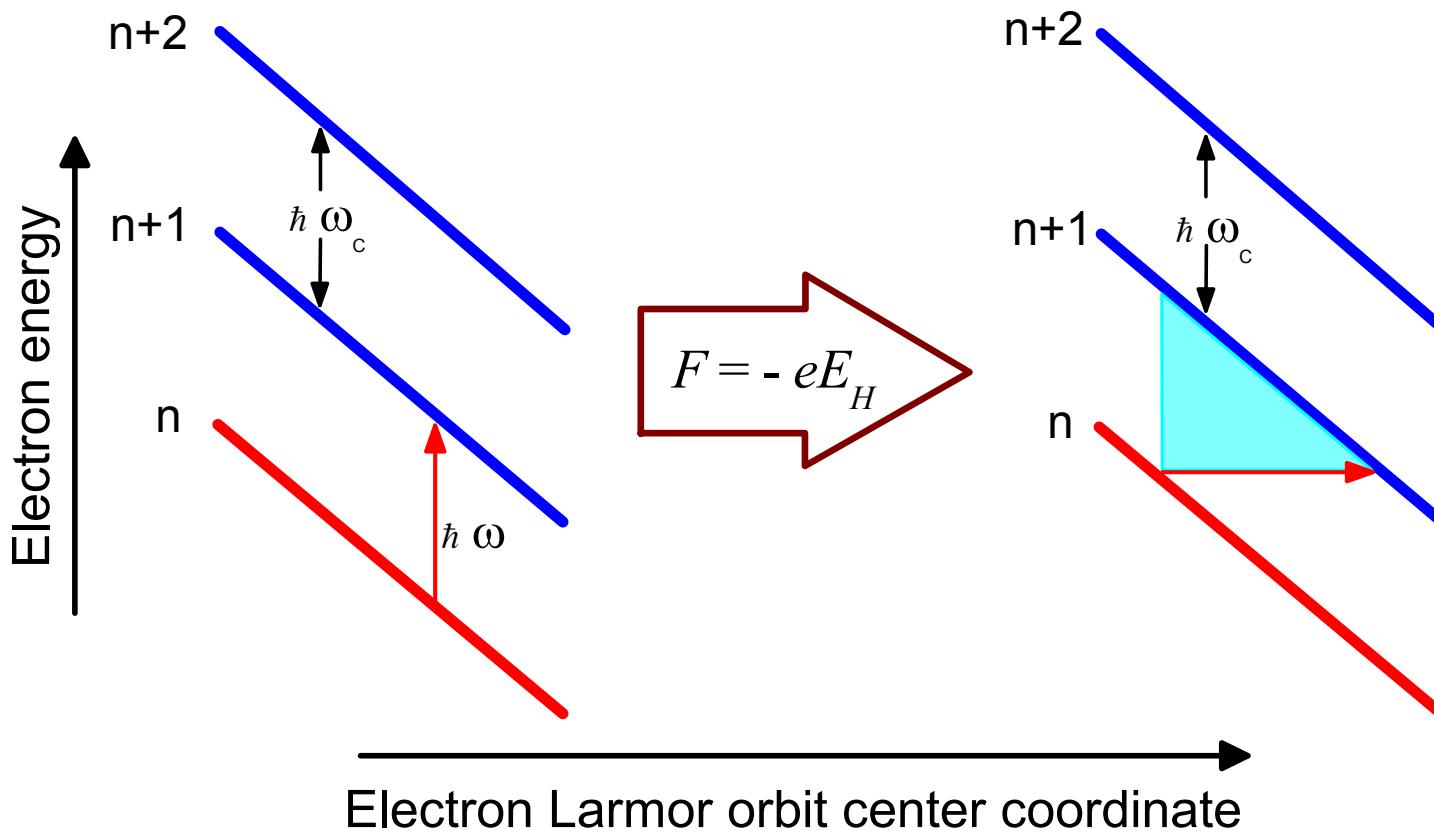


$$2R_c e E_H = l \hbar \omega_c$$

FIG. 1. The measured differential magnetoresistance traces at various dc current  $I_{dc}$  are shown for a  $50 \mu\text{m}$  Hall bar (for clarity, the traces are shifted vertically in steps of  $0.3 \text{ k}\Omega$ ). Up to three orders of oscillations are clearly seen from the traces, and the oscillations are roughly periodic in  $1/B$ . The inset is a diagram for the electrical measurement.

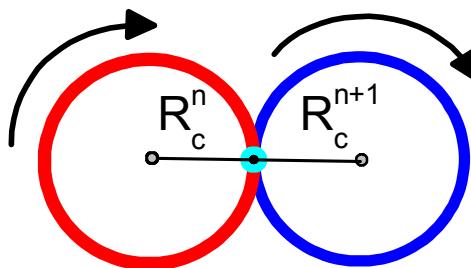
C. L. Yang et al.  
PRL, 89, 076801 (2002)

# Electron-Impurity Scattering Induced by the Microwaves or DC bias



$$2k_F u_S = l \hbar \omega_c$$

$$\hbar \omega = l \hbar \omega_c$$

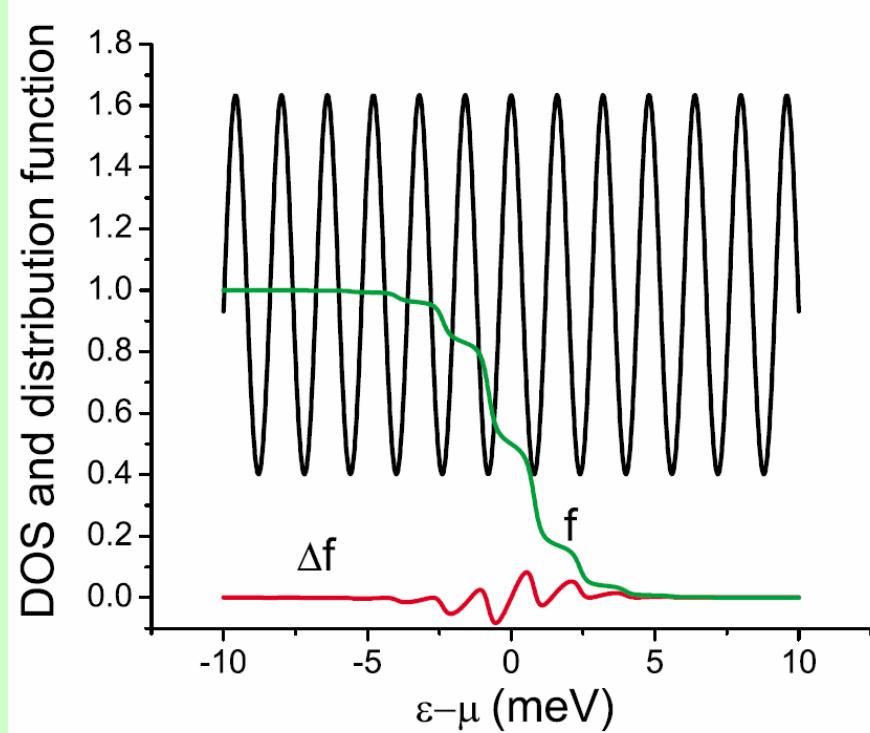
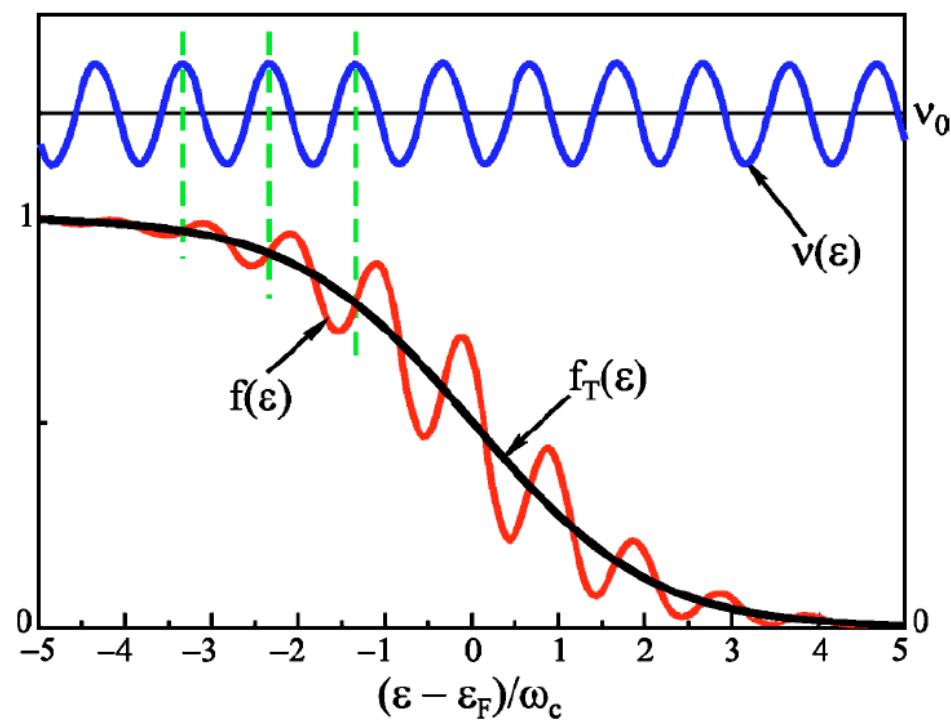


$$2R_c e E_H = l \hbar \omega_c$$

# Electron Distribution in the Energy space

$$\sigma_{\text{ph}} = \int d\varepsilon \sigma_{\text{dc}}(\varepsilon) [-\partial_\varepsilon f(\varepsilon)]$$

$$\tilde{\nu} = 1 - 2\delta \cos \frac{2\pi\varepsilon}{\omega_c}, \quad \delta = \exp\left(-\frac{\pi}{\omega_c \tau_q}\right) \ll 1$$

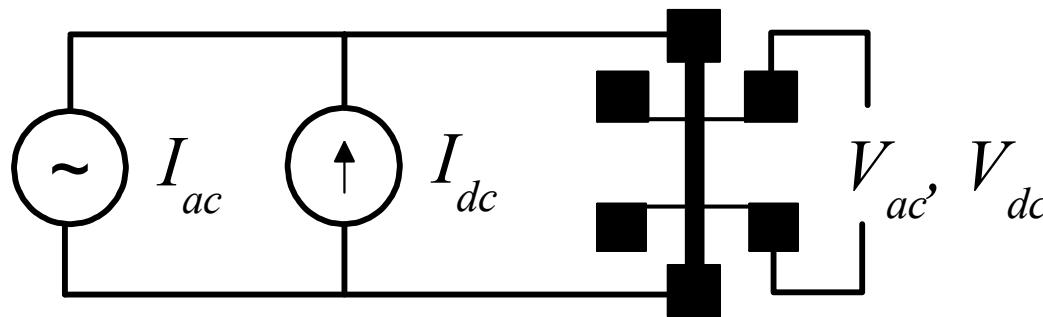


I. A. Dmitriev et al. PRB, 71, 115316 (2005).

## 2. Experiment

Samples were **GaAs quantum wells** grown by solid source molecular beam epitaxy on semi-insulating (001) GaAs substrates. Density and mobility of the 2D electrons were:

$$n_e = (0.7 - 1.2) \cdot 10^{12} \text{ cm}^{-2} \quad \text{and} \quad \mu = (0.5 - 2) \cdot 10^6 \text{ cm}^2/\text{Vs.}$$



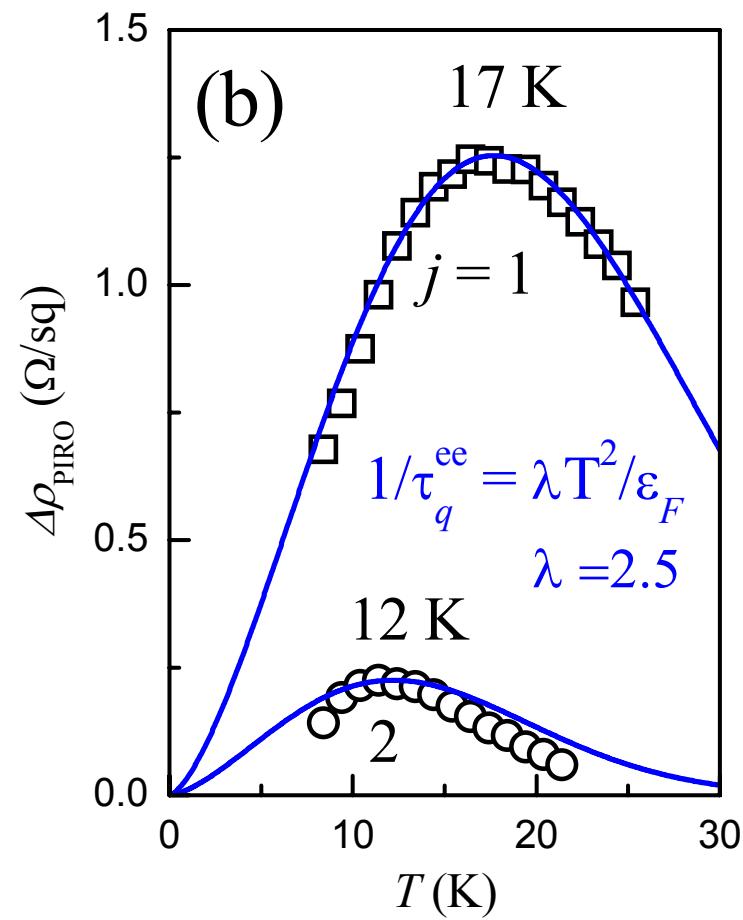
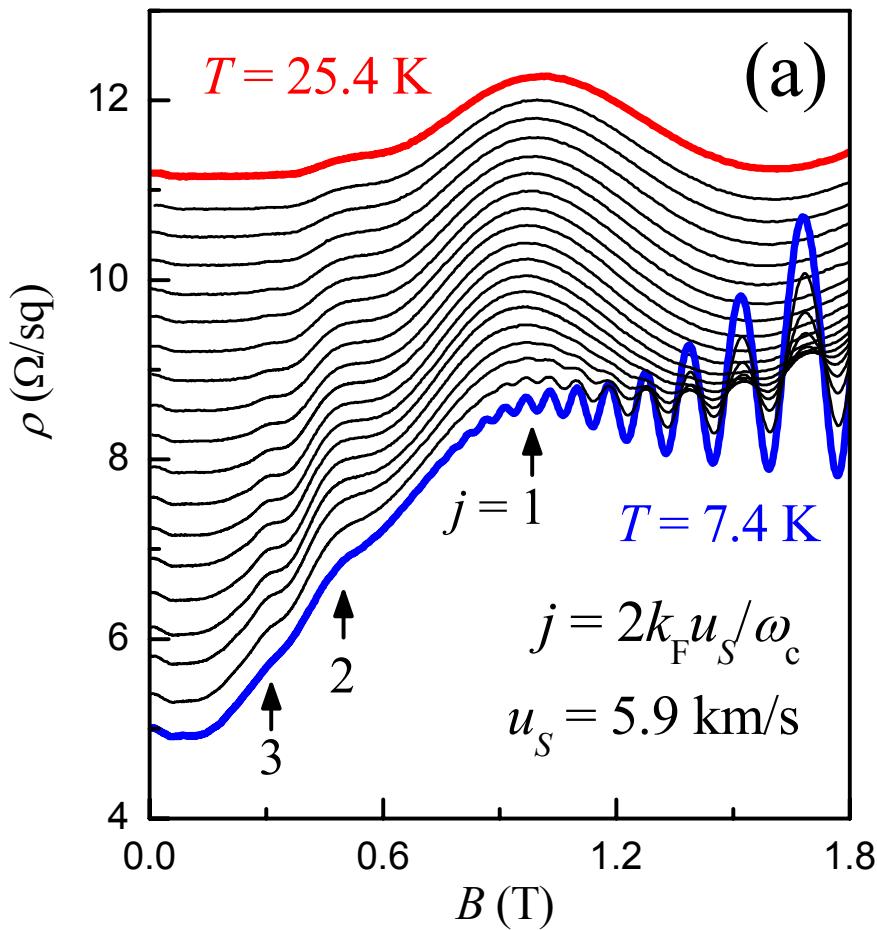
$$F = 1 - 140 \text{ GHz}$$

$$\begin{aligned} & V_{dc}(I_{dc}) \\ & V_{dc}/I_{dc} = R_0 \\ & V_{ac}/I_{ac} = r_{xx} \\ & V_{ac}^{(0)}, V_{ac}^{(1)} \\ & V_{ac}^{(2)}, V_{ac}^{(3)} \end{aligned}$$

$$V = R_0 I_{dc} + V^{(0)} + V^{(1)} + V^{(2)} + V^{(3)} + \dots$$

### 3. Results

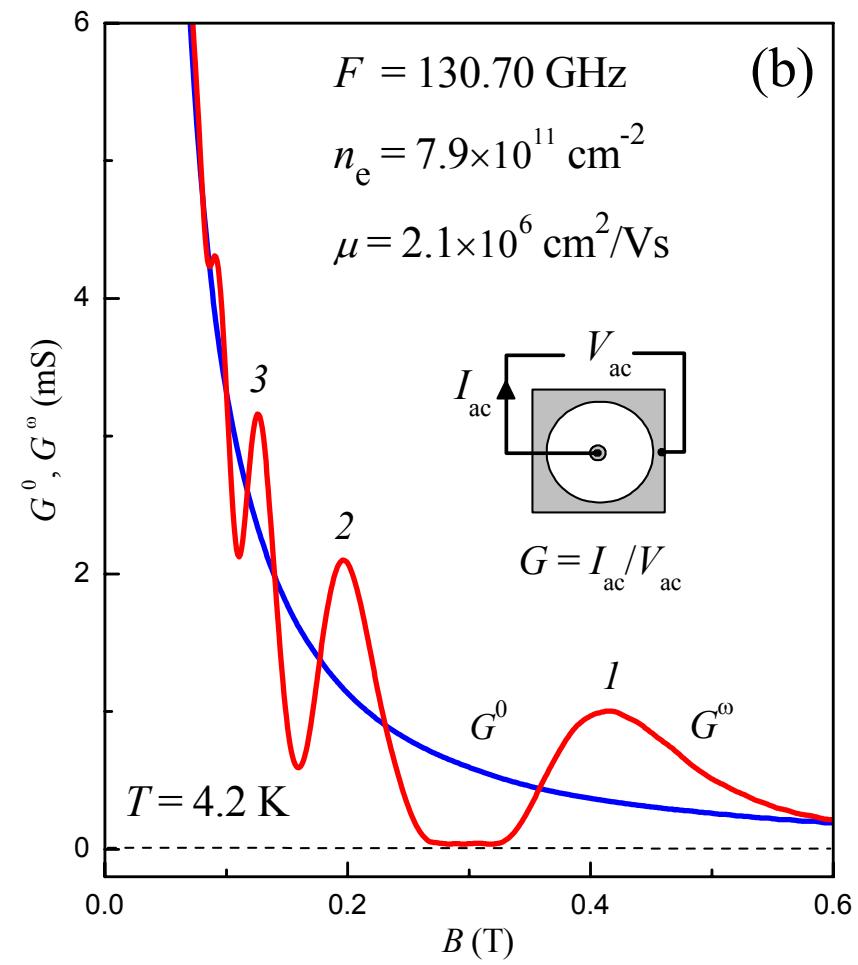
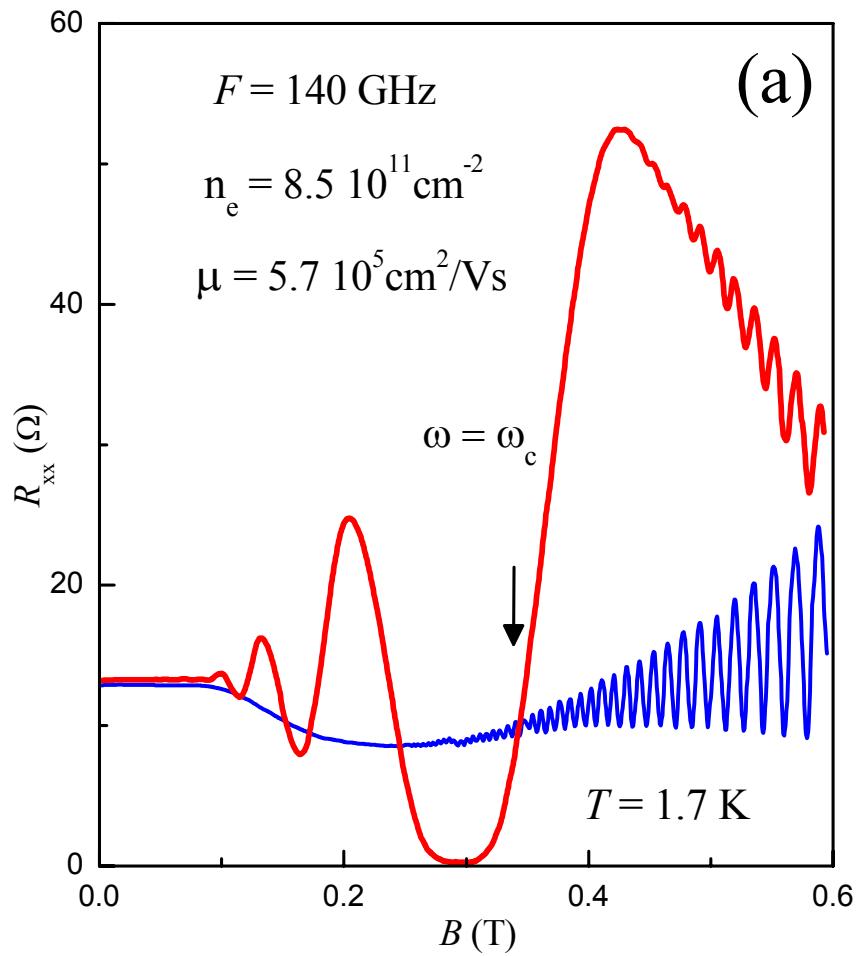
## Phonon-Induced Resistance Oscillations



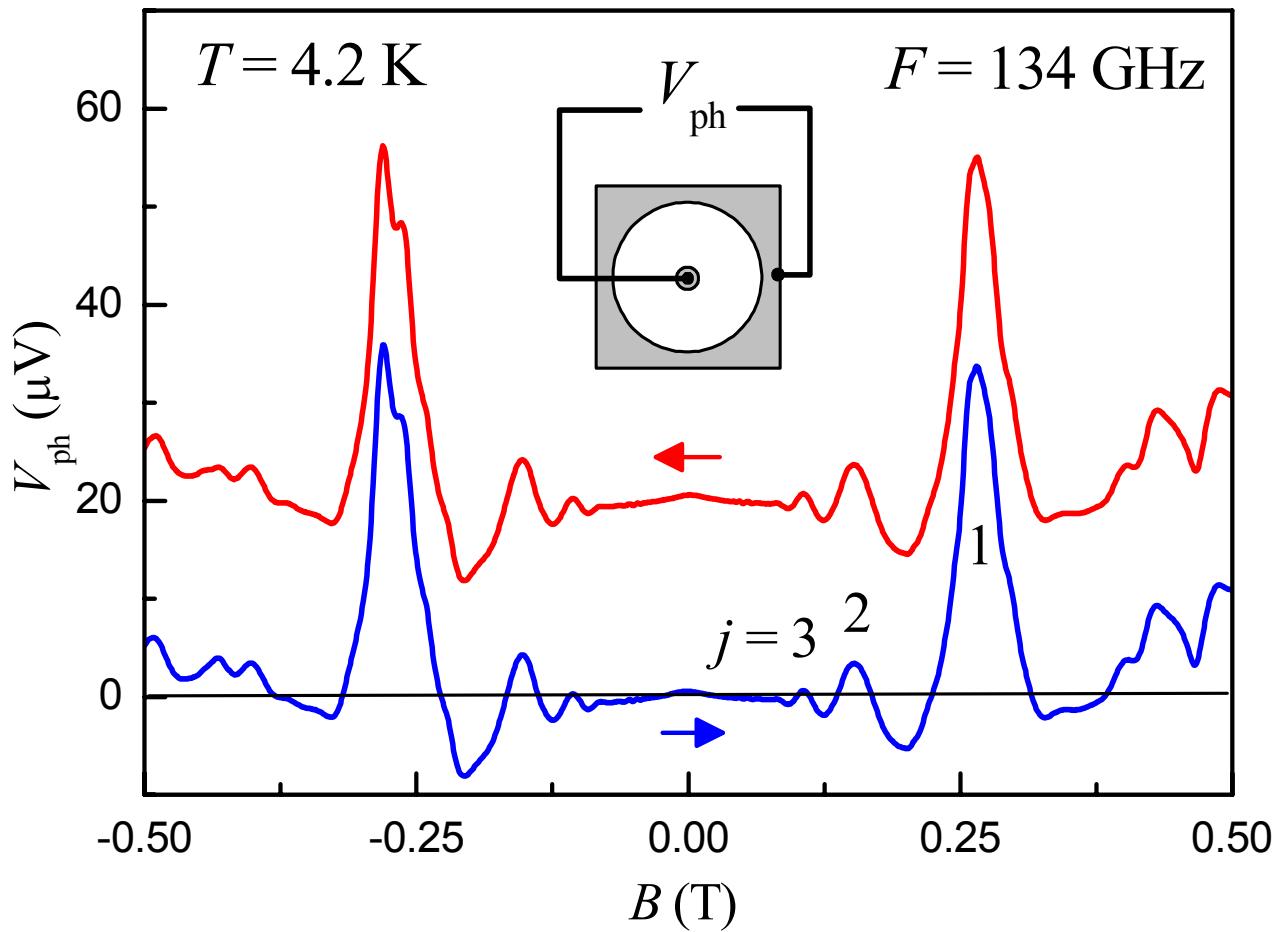
A. A. Bykov et al. JETP Letters, **81**, 553 (2005), JETP Letters, **90**, 578 (2009).

Theory: O. E. Raichev. PRB, **80**, 075318 (2009).

# Microwave-Induced Resistance and Conductance Oscillations



# Microwave-Induced Photovoltage Oscillations

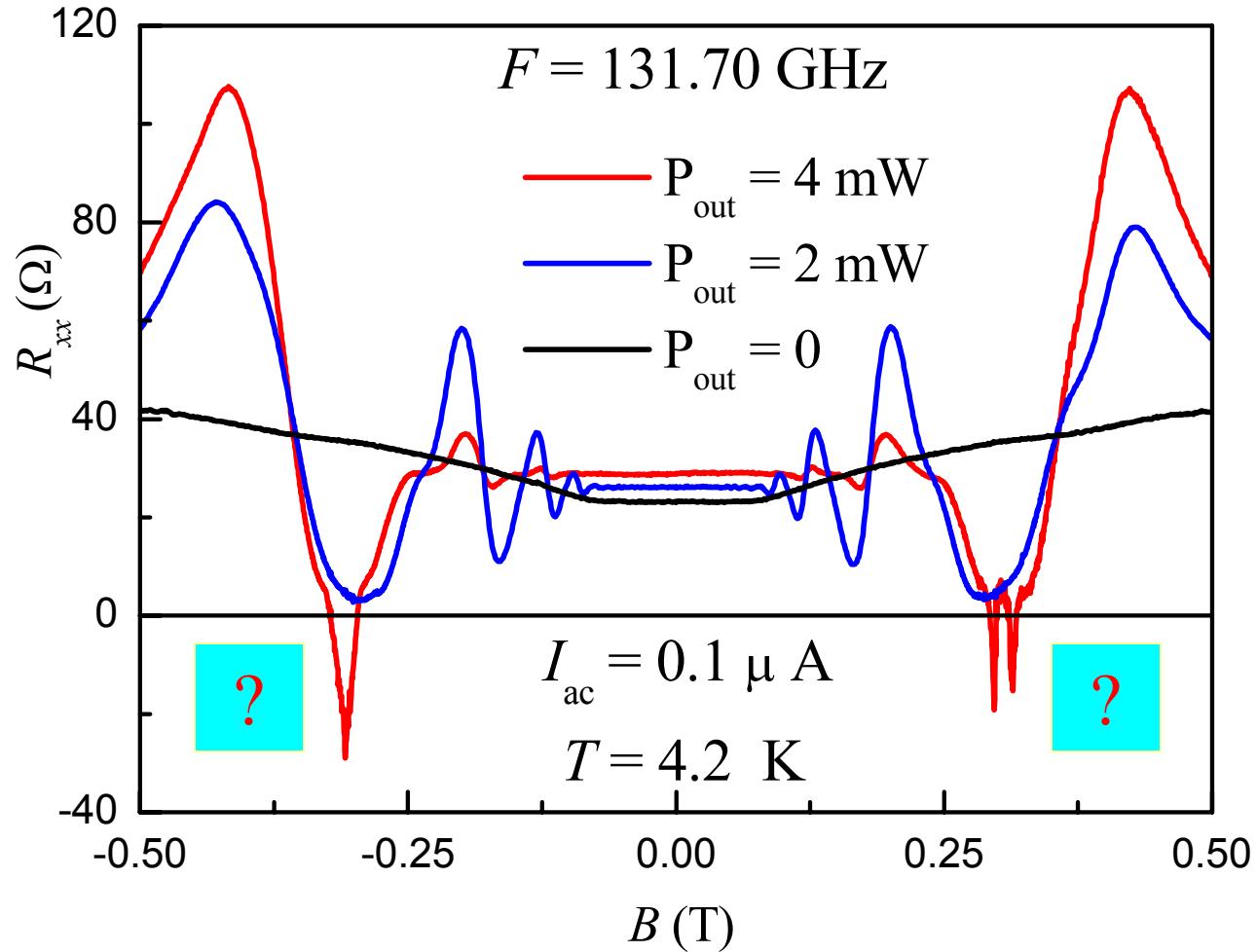


R. L. Willet  
et al.  
PRL, 93, 026804  
(2004).

A. A. Bykov.  
JETP Letters,  
87, 233  
(2008).

S. I. Dorozhkin  
et al.  
PRL, 102,  
036602  
(2009).

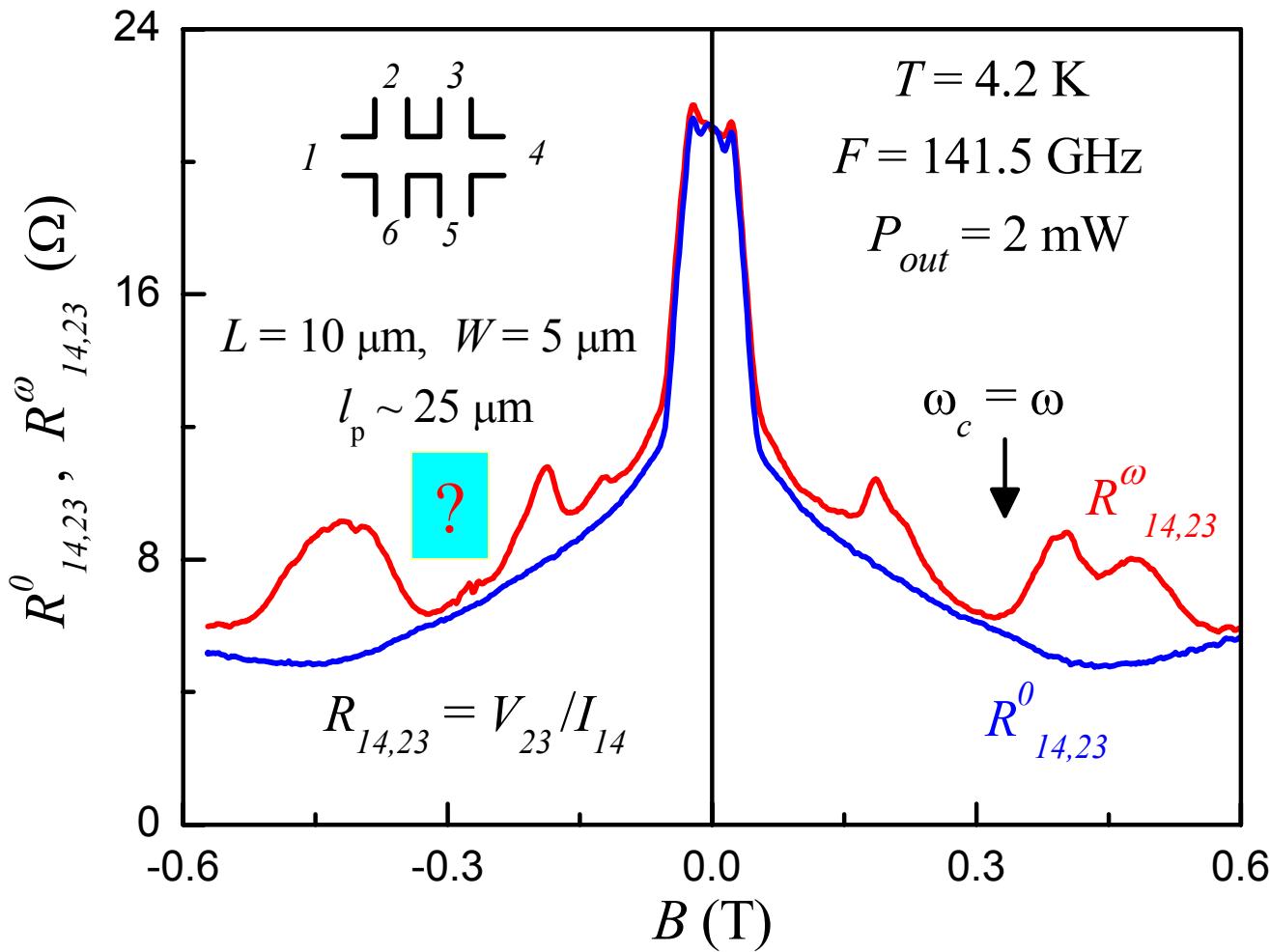
# Microwave-Induced Absolute Negative Resistance in a 2D Electron System



R. L. Willet  
et al.  
PRL, 93, 026804  
(2004).

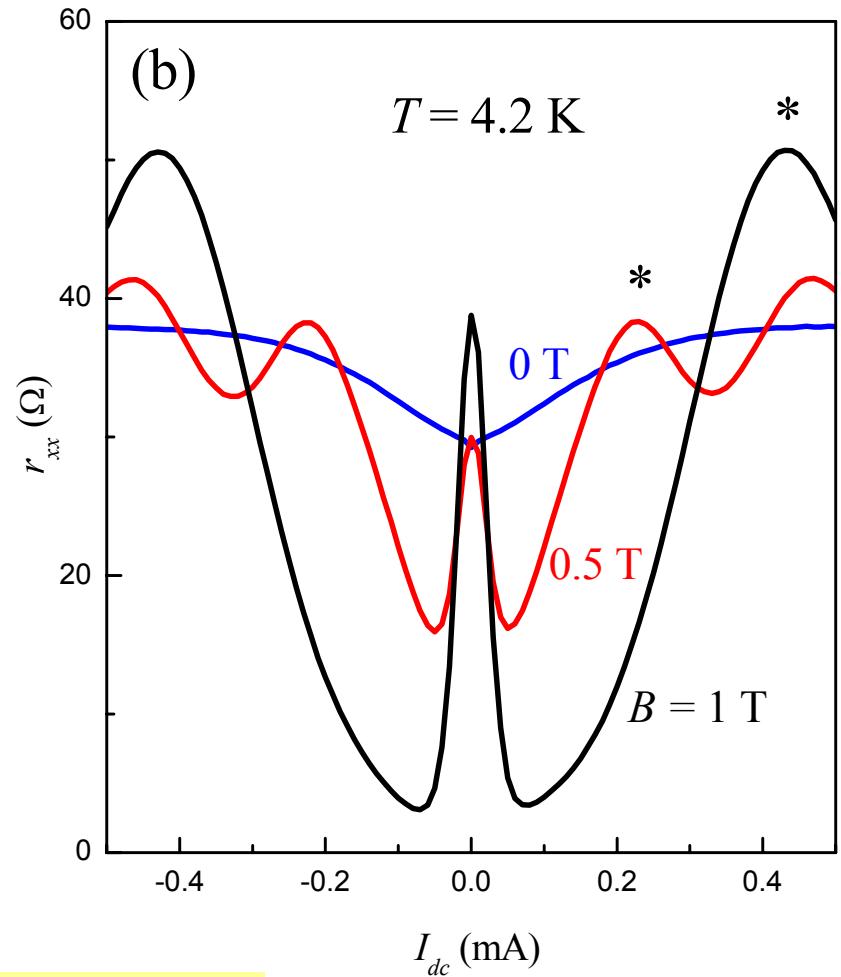
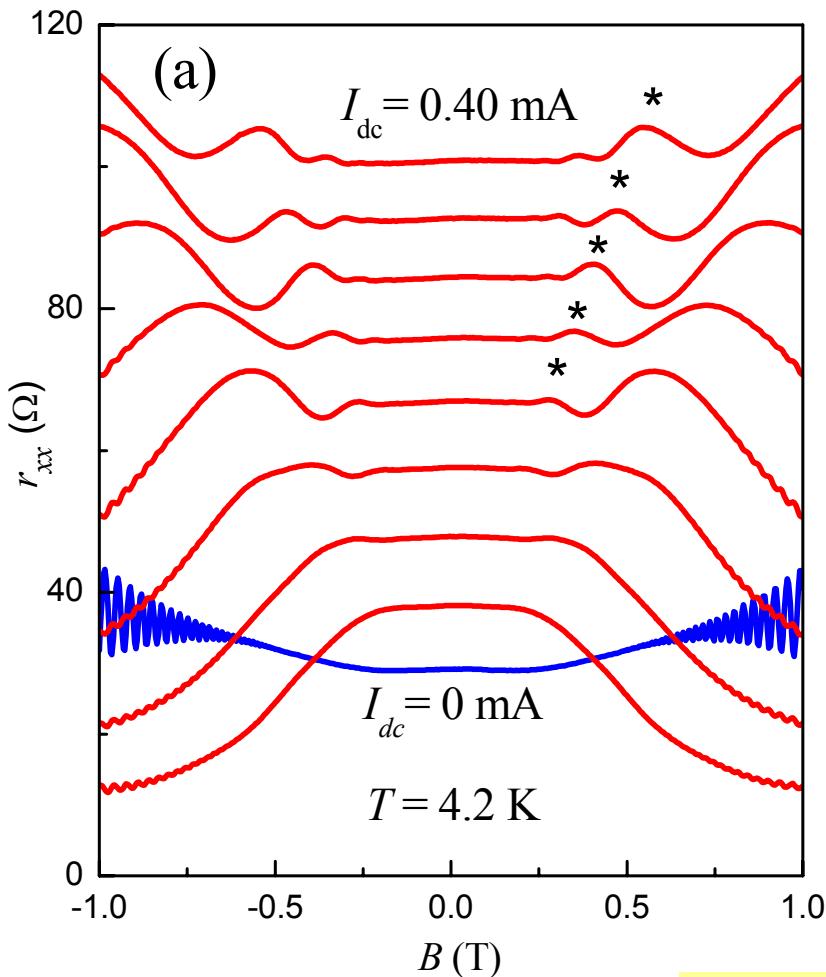
M. A. Zudov  
et al.  
PRB, 73, 041303  
(2006).

# Microwave-Induced Resistance Oscillations in a Ballistic Microbar



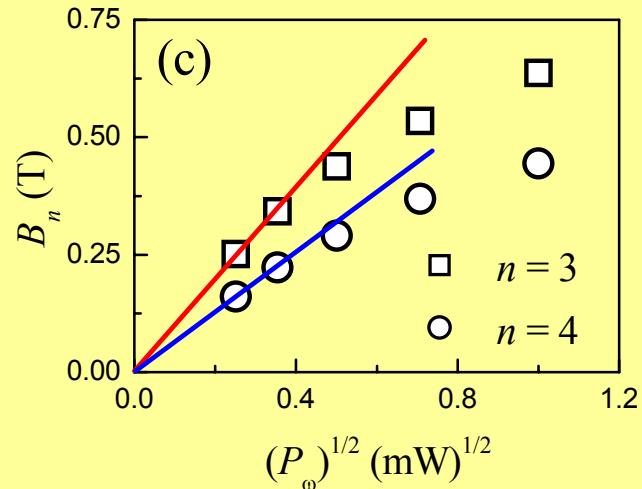
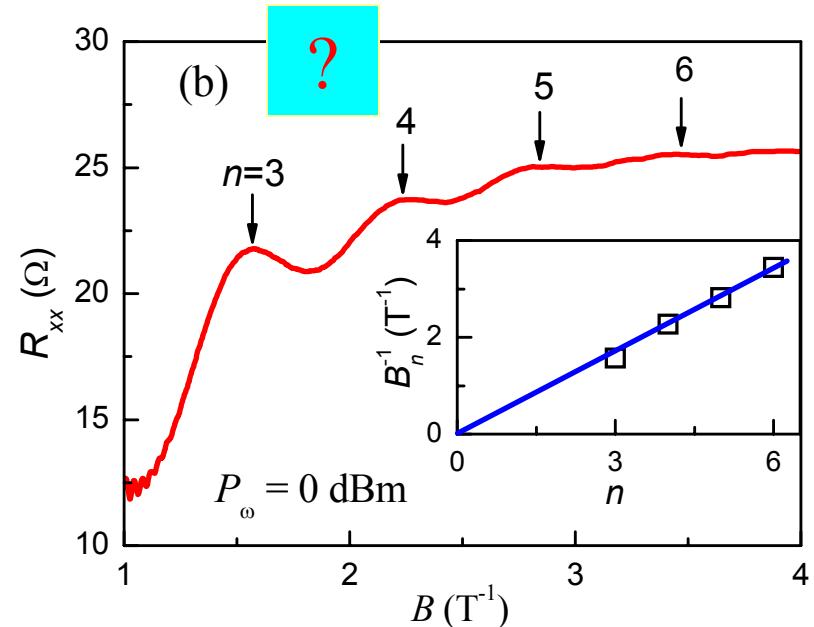
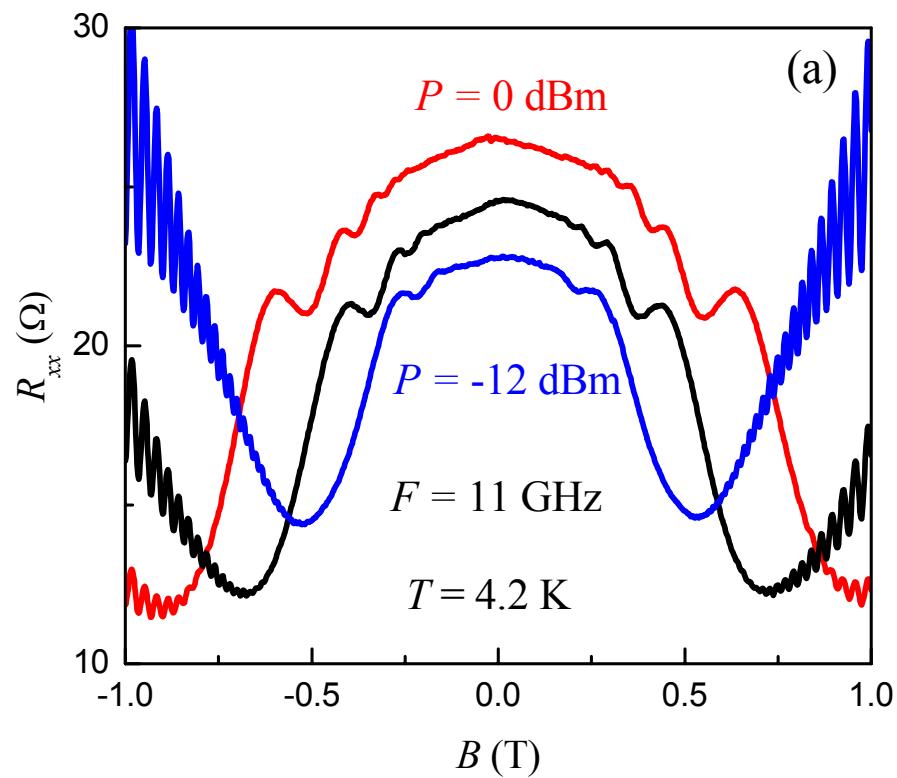
**Theory:**  
A. D. Chepelianskii,  
D. L. Shepelyansky  
PRB, **80**, 241308 (R)  
(2009).

# Hall Field-Induced Resistance Oscillations



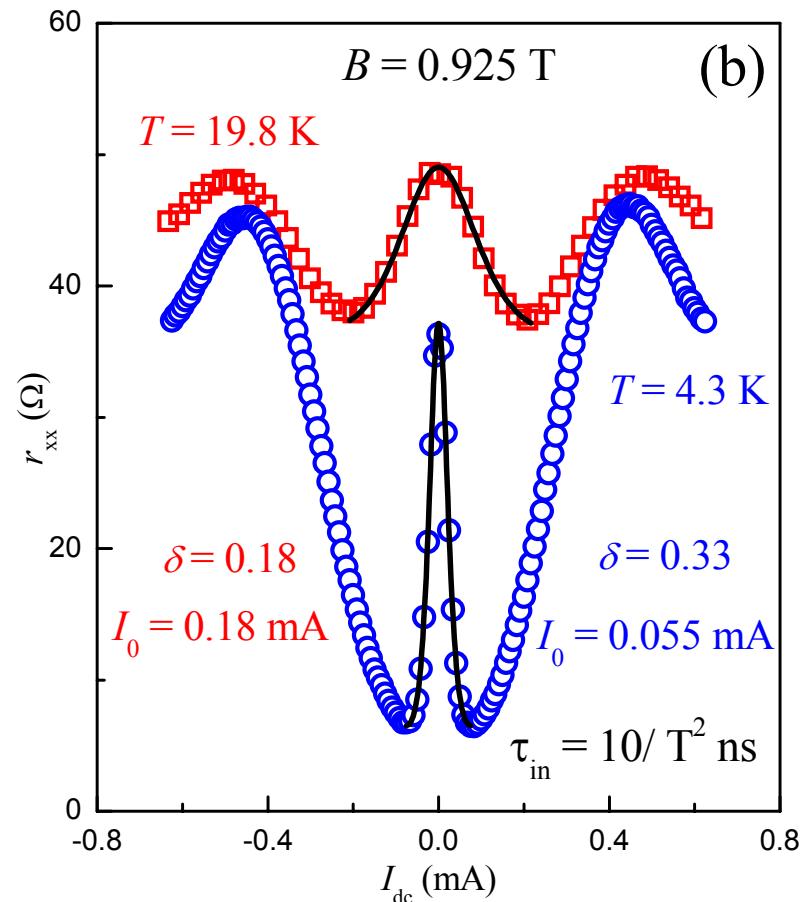
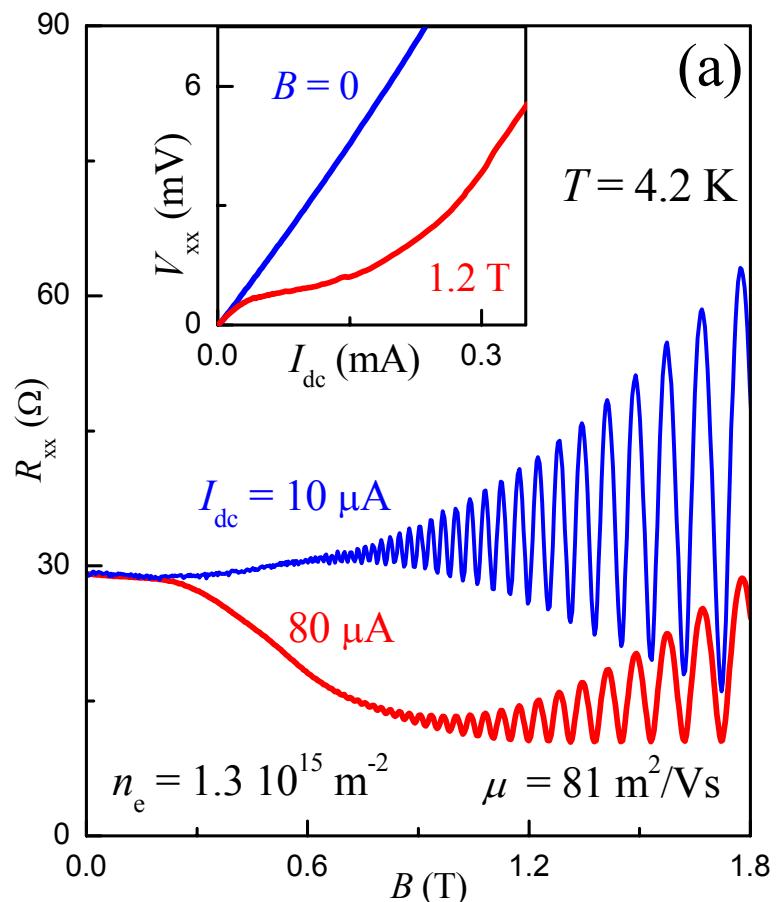
$$2R_c e E_H = l\hbar\omega_c$$

# AC excitation 11 GHz



For a linear microwave circuit current density through the sample should be proportional to square root of the input microwave power  $J_\omega \sim (P_\omega)^{1/2}$ .

# Effect of a DC Electric Field on the Longitudinal Resistance

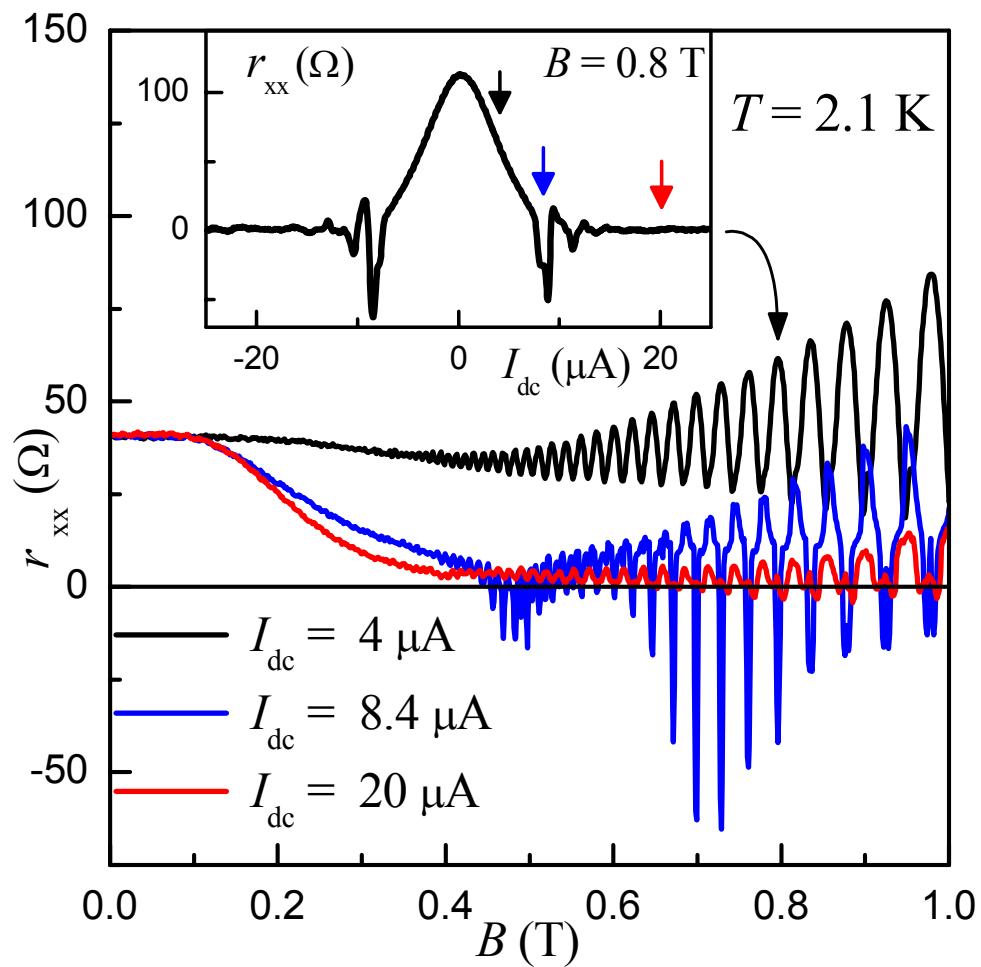


J. Q. Zhang et al. PRB, **75**, 081305 (2007).

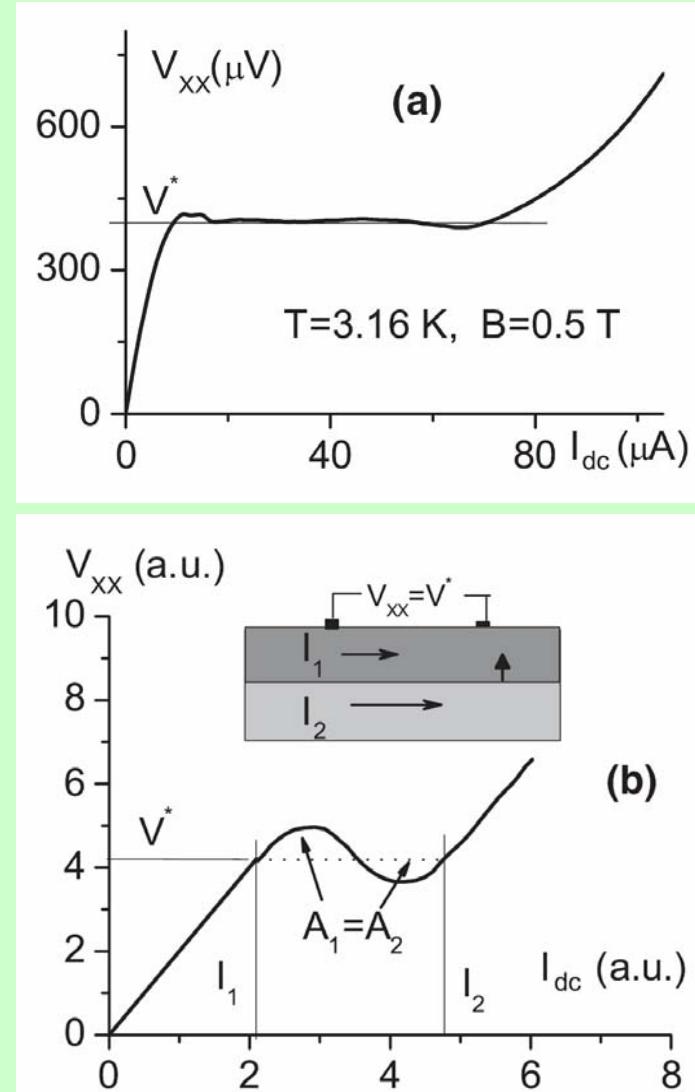
A. A. Bykov et al.  
JETP Letters, **81**, 406 (2005).

Theory: I. A. Dmitriev et al.  
PRB, **71**, 115316 (2005).

# Zero-Differential Resistance State

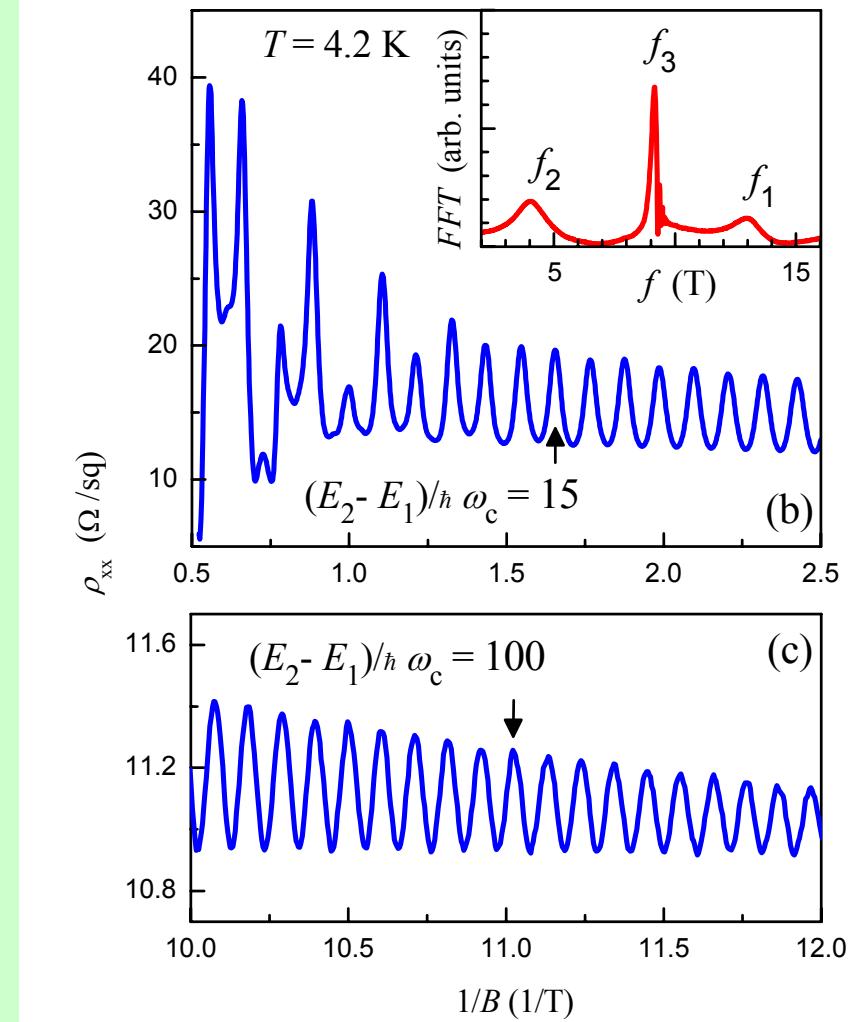
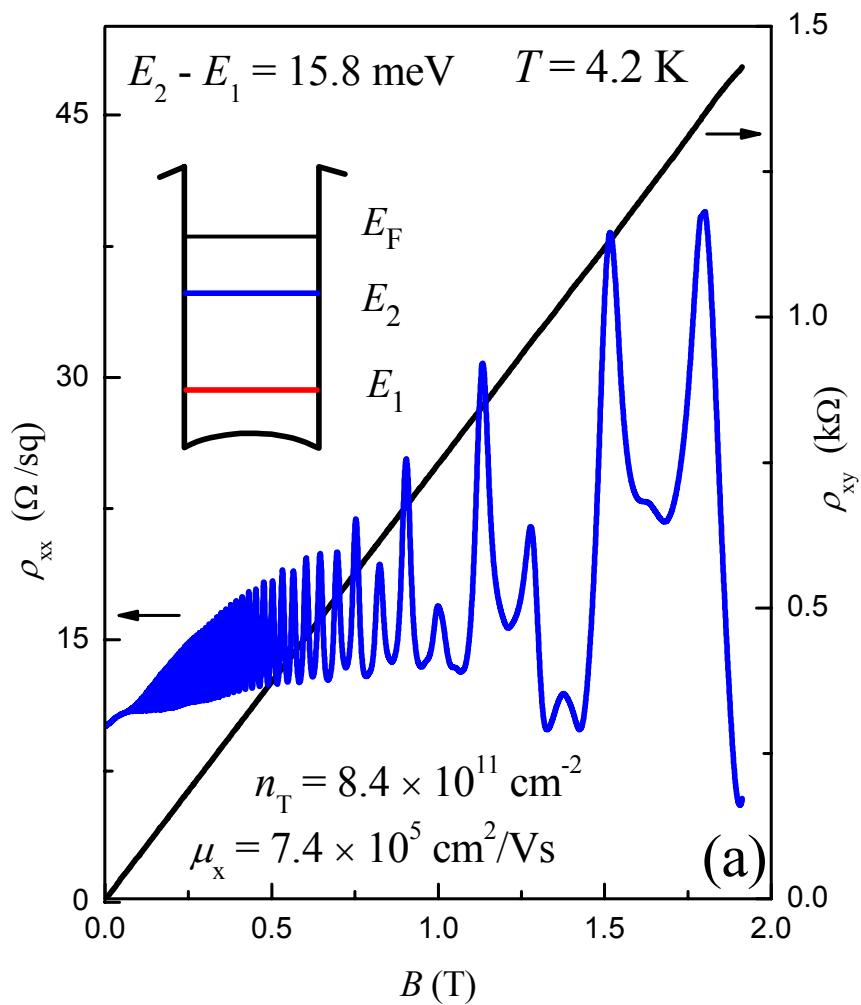


N. Romero Kalmanovitz et al.  
PRB, 78, 085306 (2008).



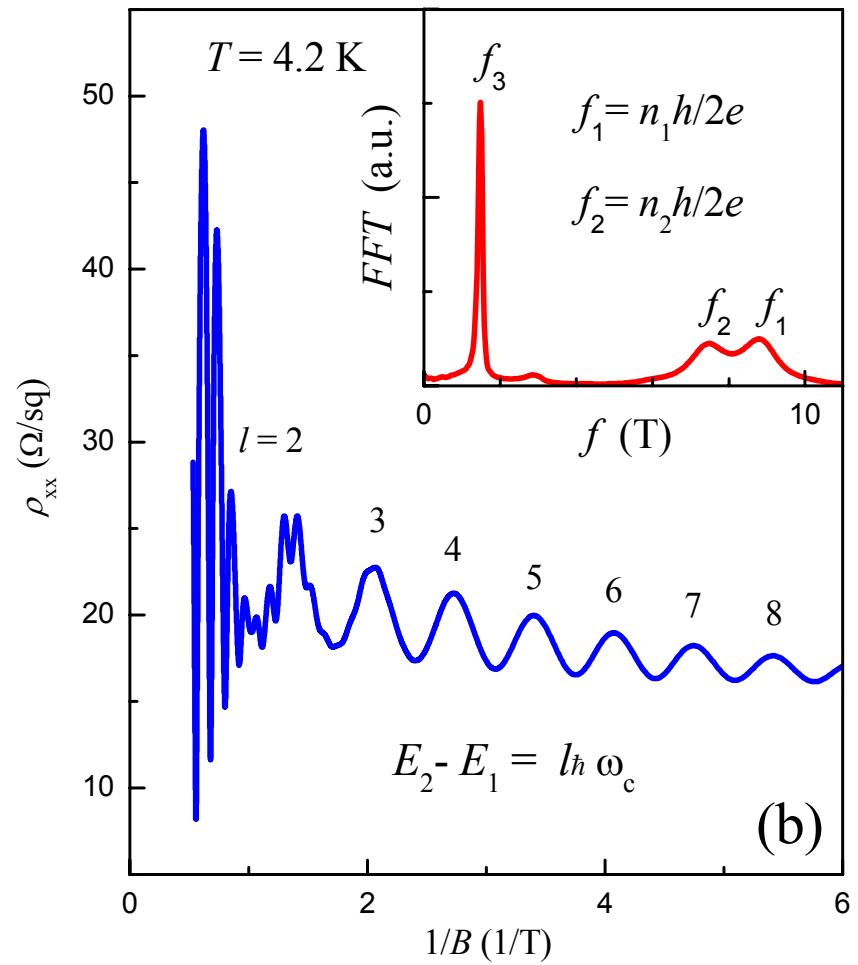
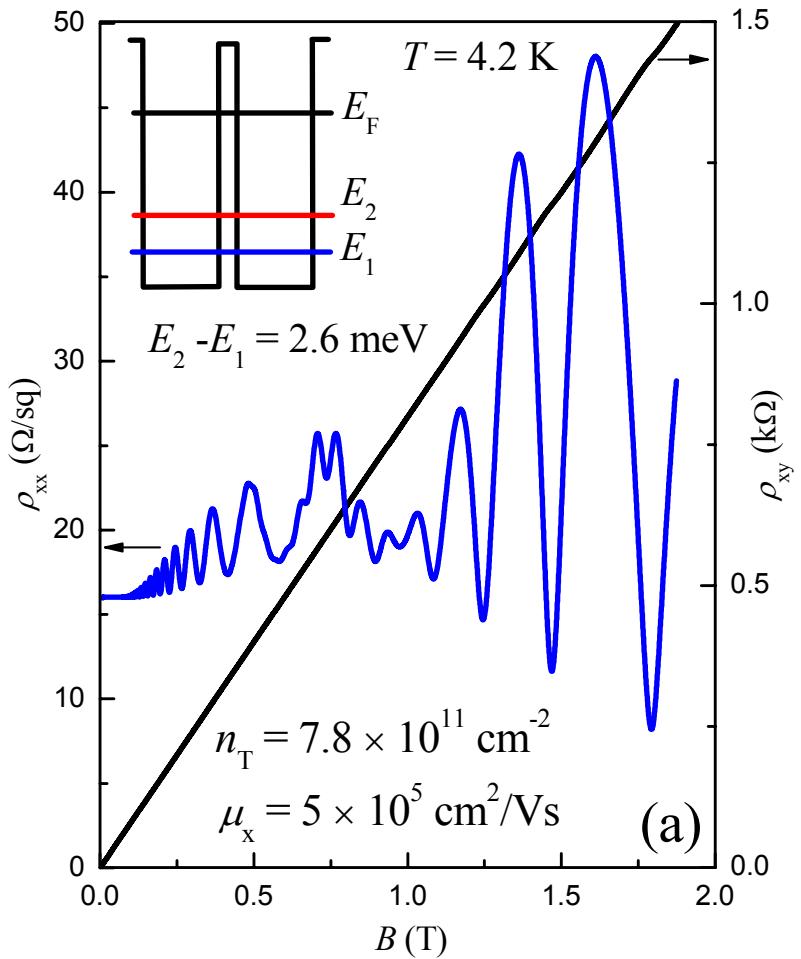
A. A. Bykov et al.  
PRL, 99, 116801 (2007).

# Single Quantum Well With Two Populated Subbands



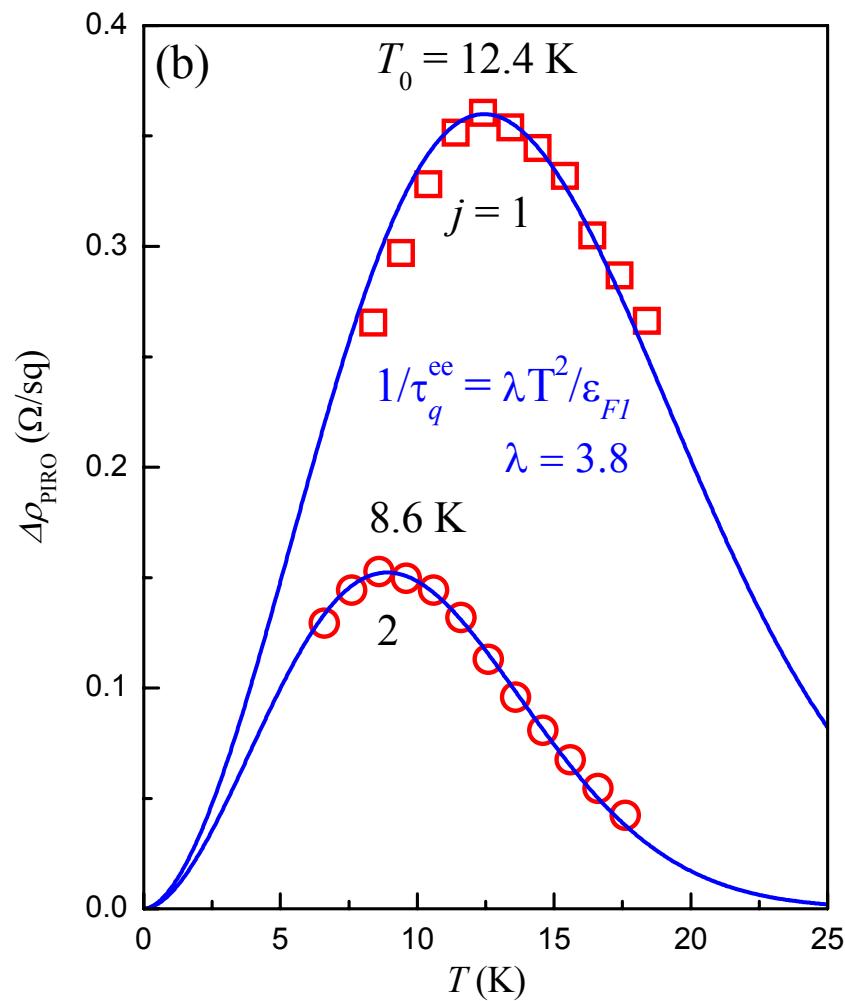
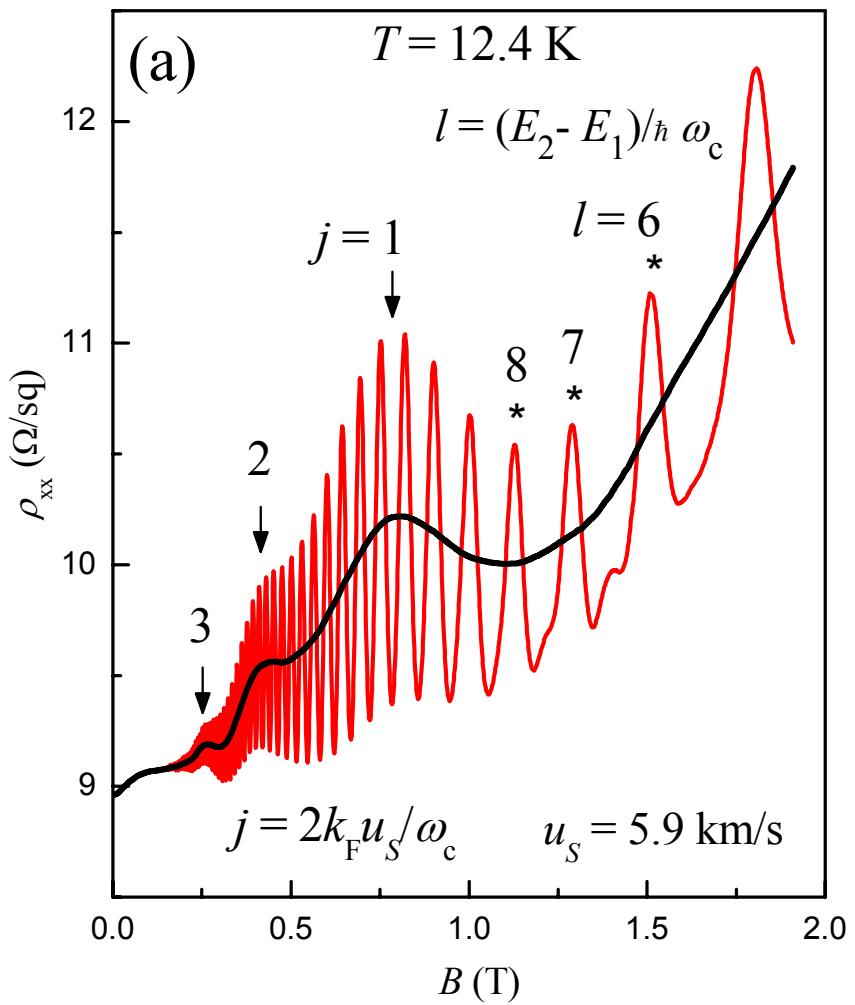
A. V. Goran et al. PRB, **80**, 193305 (2009).

# Duble Quantum Well With Two Populated Subbands

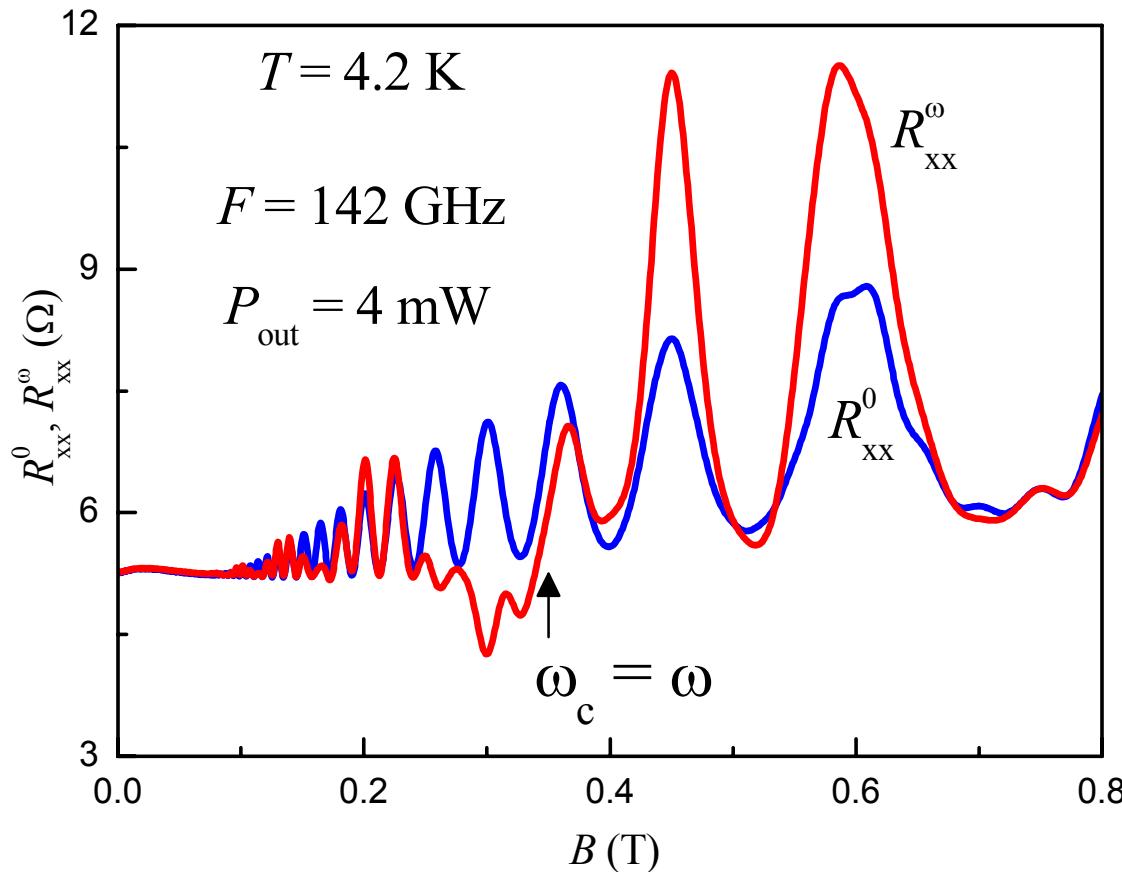


A. A. Bykov et al. JETP Letters, 88, 64 (2008).

# Phonon-Induced Resistance Oscillations in single quantum wells with two populated subbands



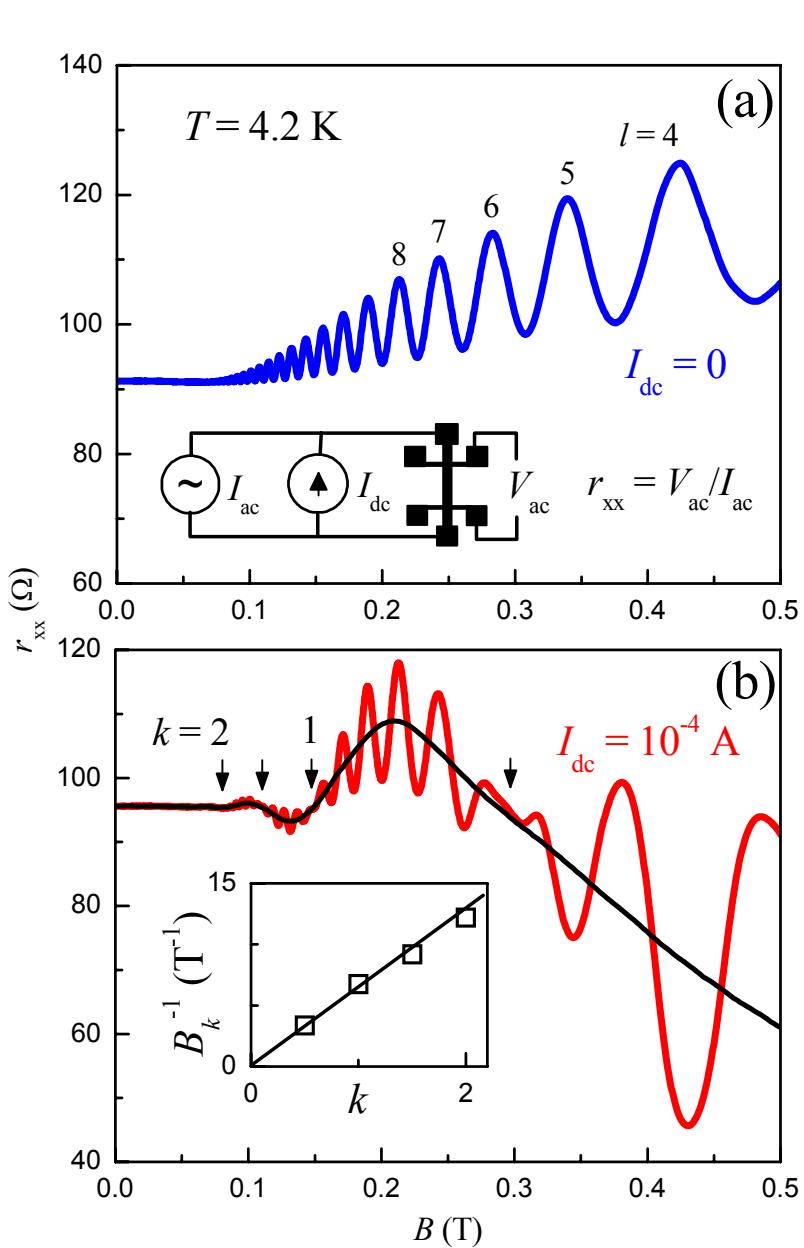
# Microwave-Induced Resistance Oscillations in Double Quantum Wells



A. A. Bykov et al. JETP Letters,  
87, 477 (2008).

S.Wiedman, G.Gusev, O.Raichev et al.  
PRB, 78, 121301(R) (2008).

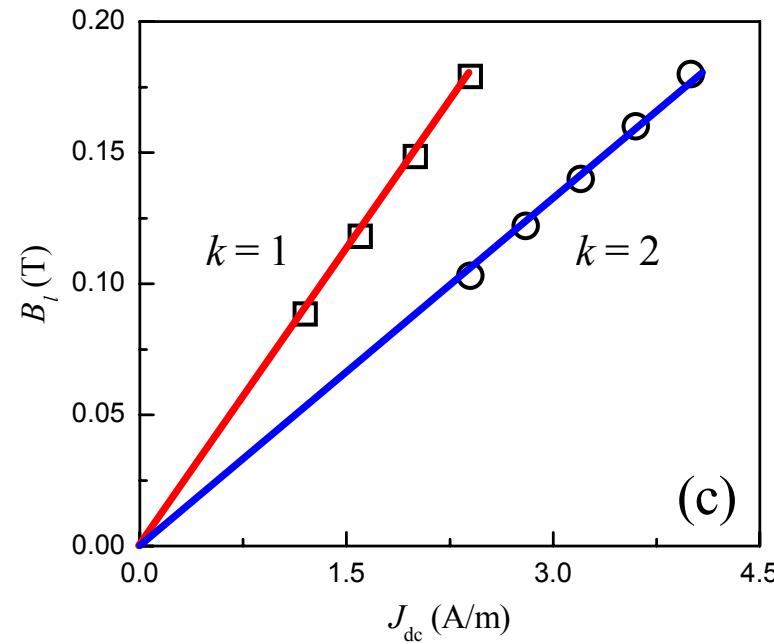
# Туннелирование Зинера в двойной квантовой яме



$$\omega_H/\omega_c = k$$

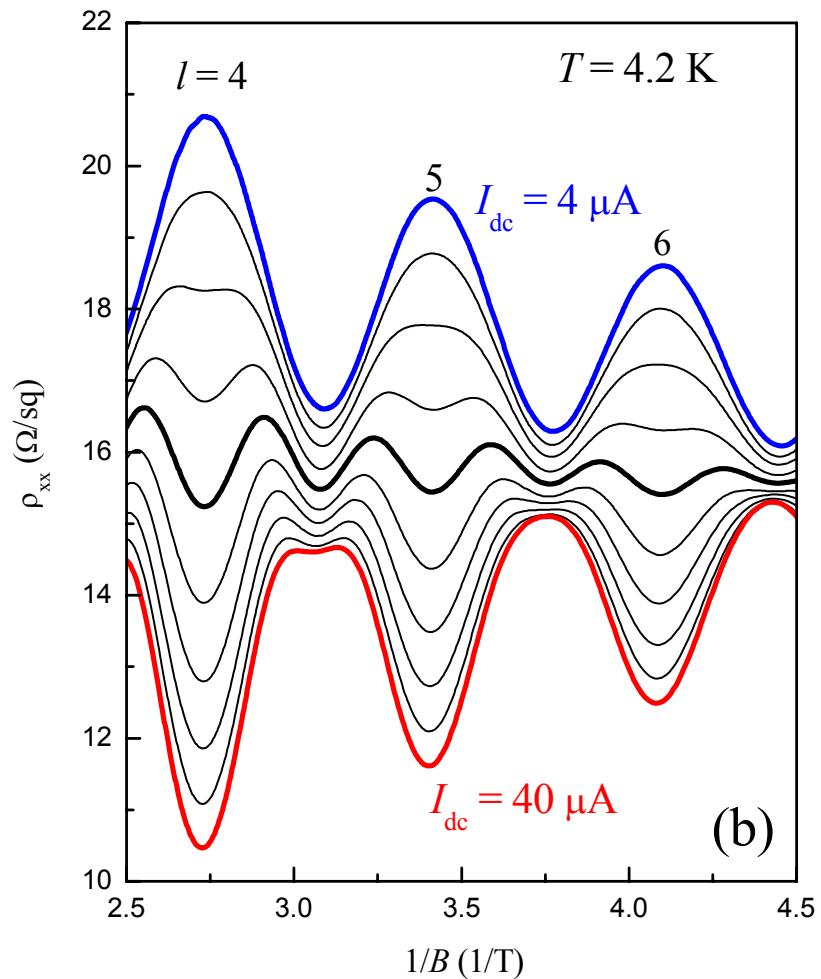
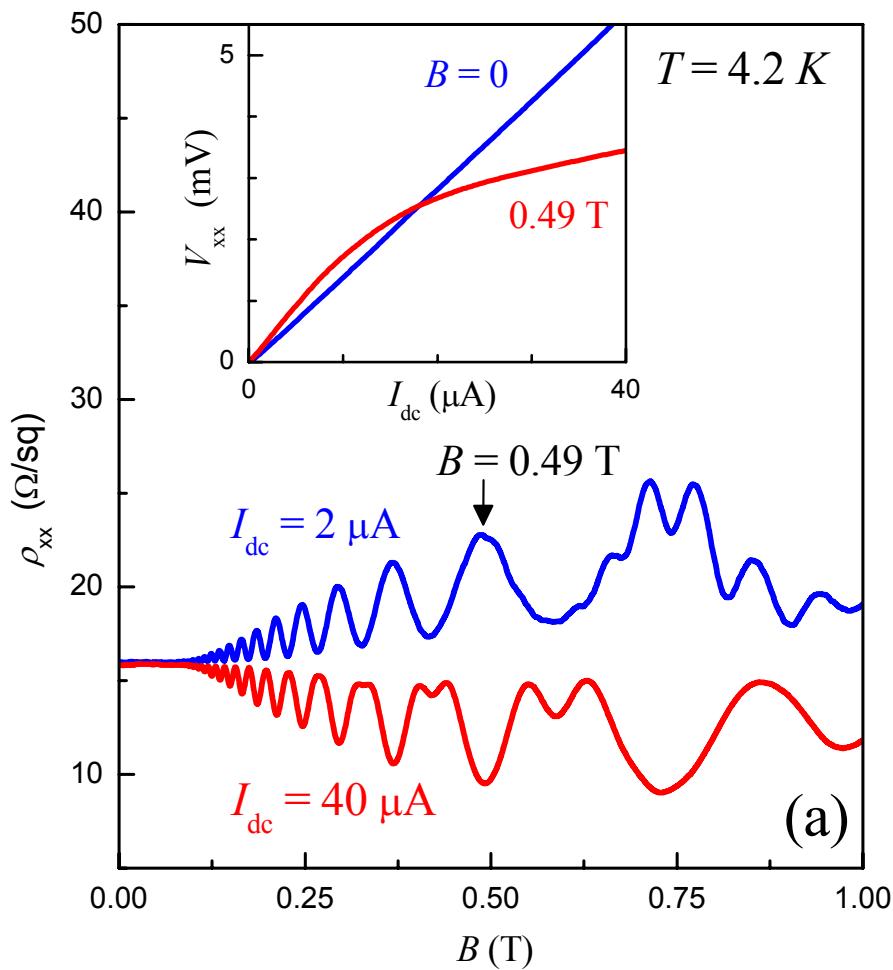
$$\omega_H = e\gamma R_c E_H \hbar$$

$$\omega_H \sim \gamma e^{-1} (\pi/n_T)^{1/2} J_{dc}$$



A. A. Bykov. JETP Letters, 88, 394 (2008).

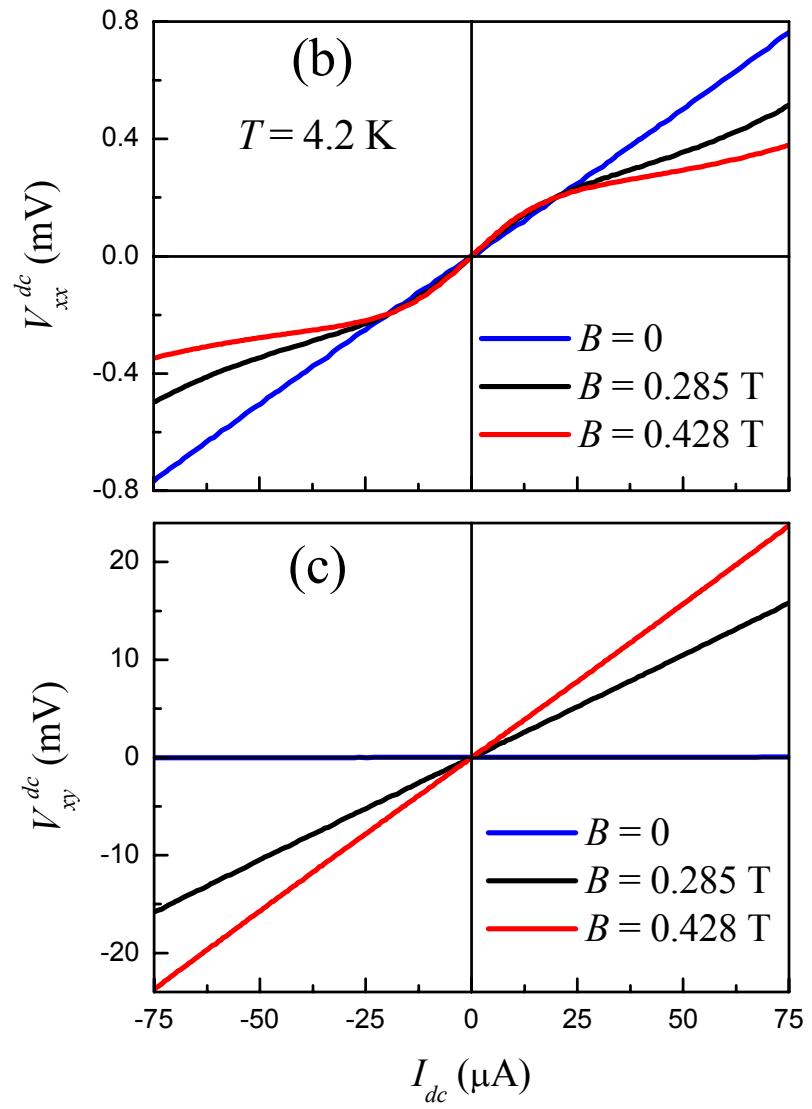
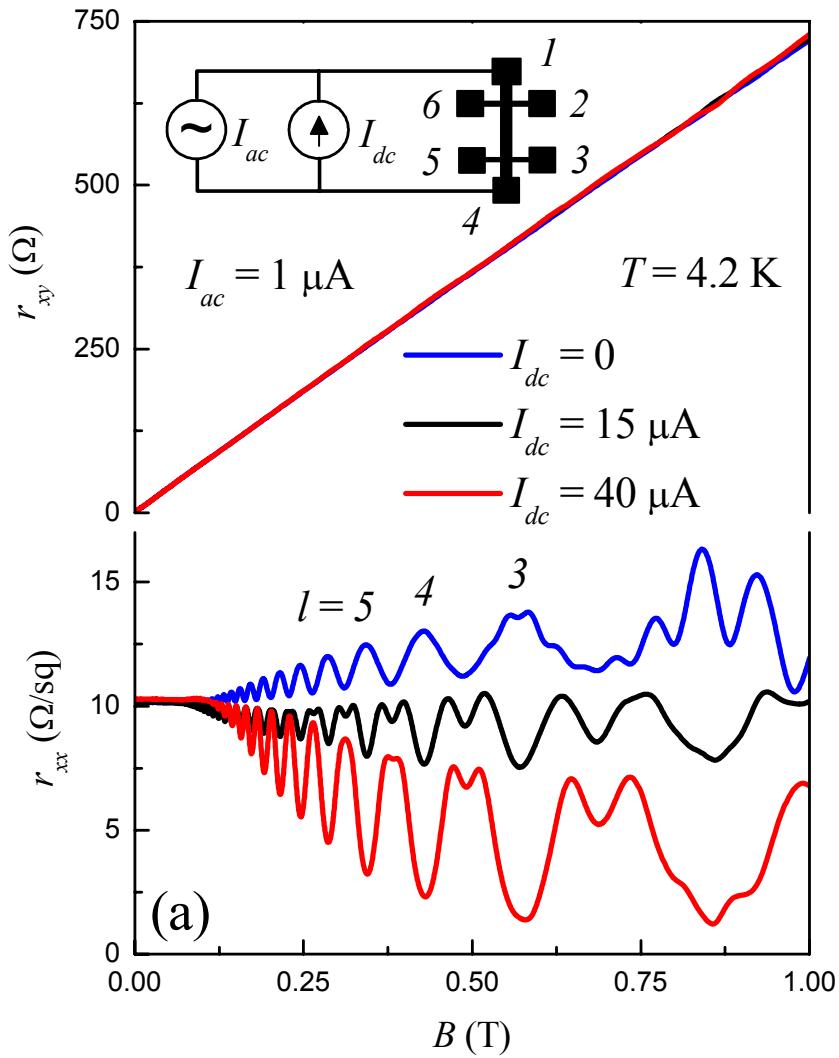
# Инверсия магнето-межподзонных осцилляций



A. A. Bykov. JETP Letters,  
88, 64 (2008).

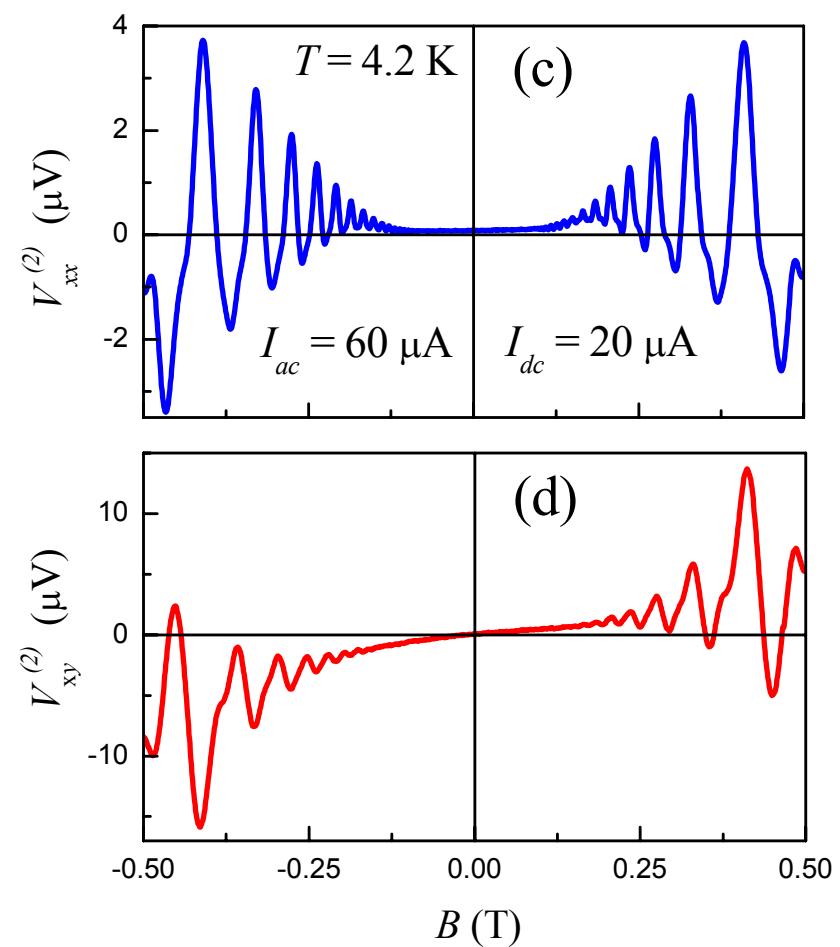
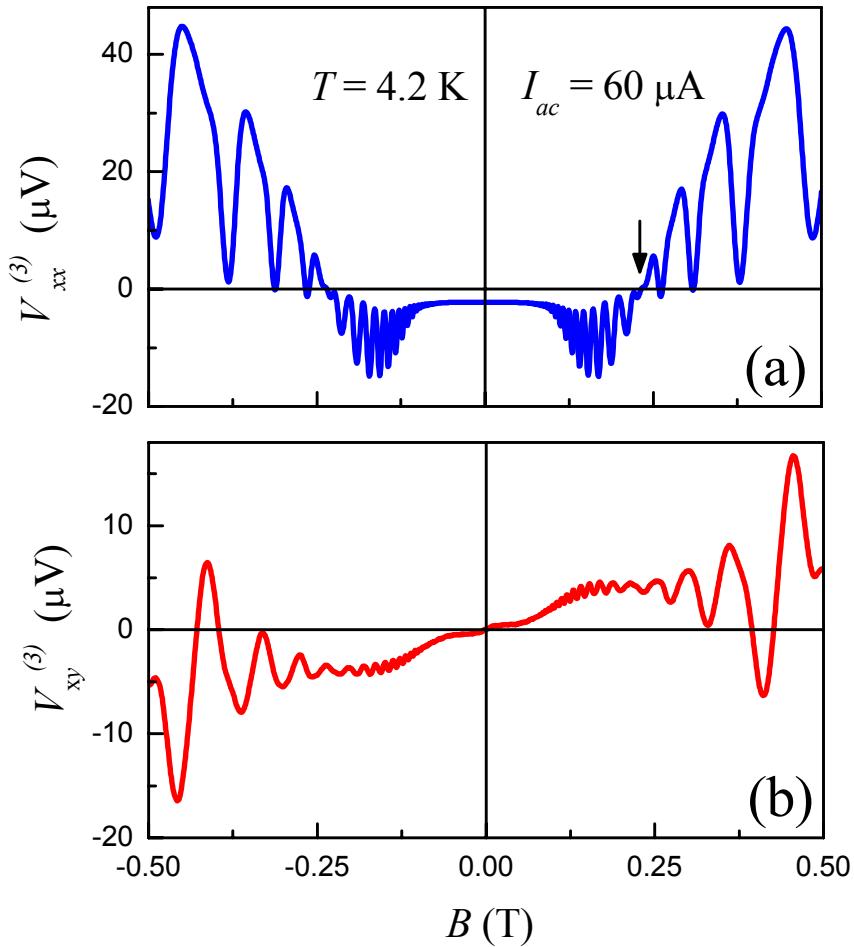
N.Mamani, G.Gusev, O.Raichev et al.  
PRB, 80, 075308 (2009).

# Дифференциальное сопротивление и ВАХ

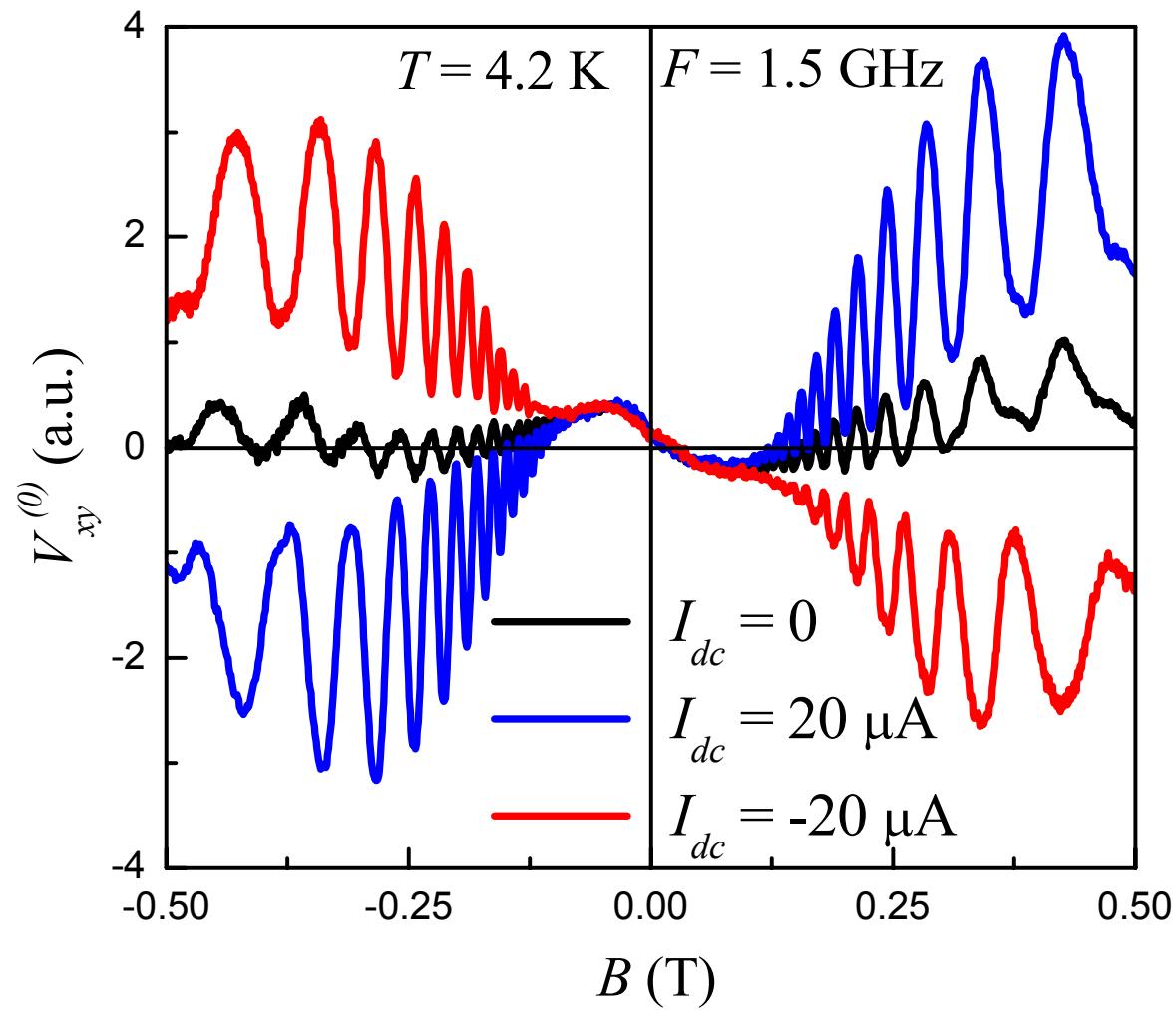


# Генерация гармоник в двойной квантовой яме

$$V = R_0 I_{dc} + V^{(0)} + V^{(1)} + V^{(2)} + V^{(3)} + \dots$$



# ЭДС Холла в двойной квантовой яме



A. A. Bykov. JETP Letters, **89**, 461 (2009).

## 4. Conclusion